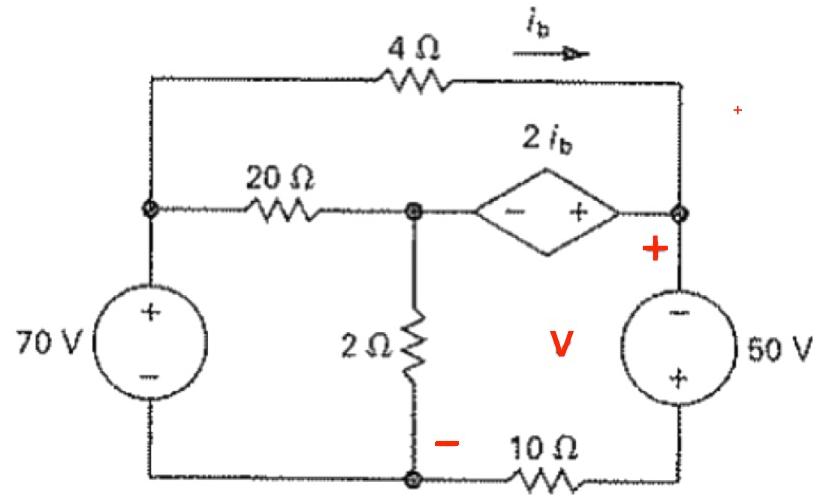


Mesh Analysis

concept; examples

General Methods to Analyze Circuits

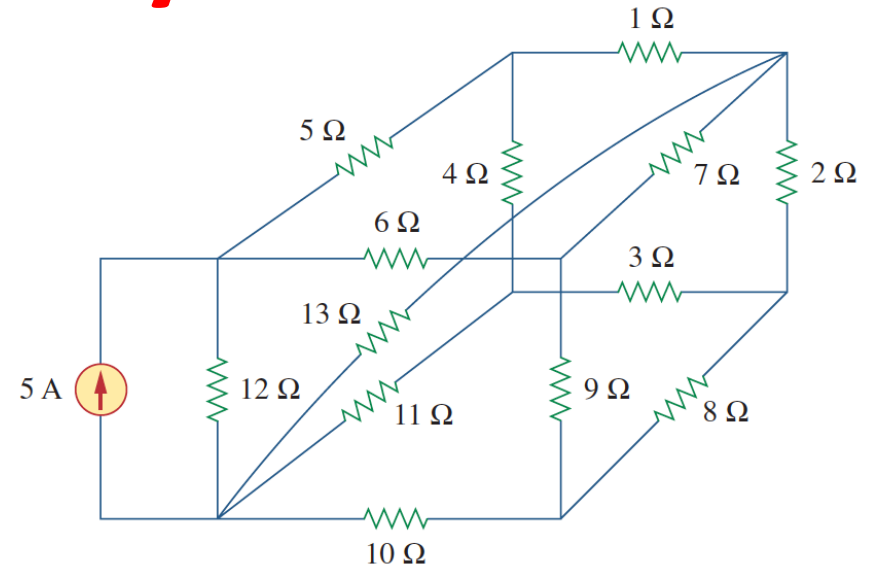
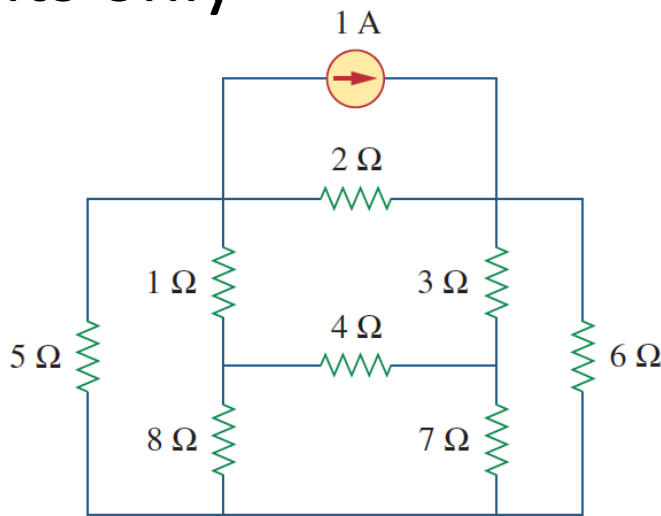
- What to do first?
 - KVL?
 - KCL?
 - Ohm's Law?



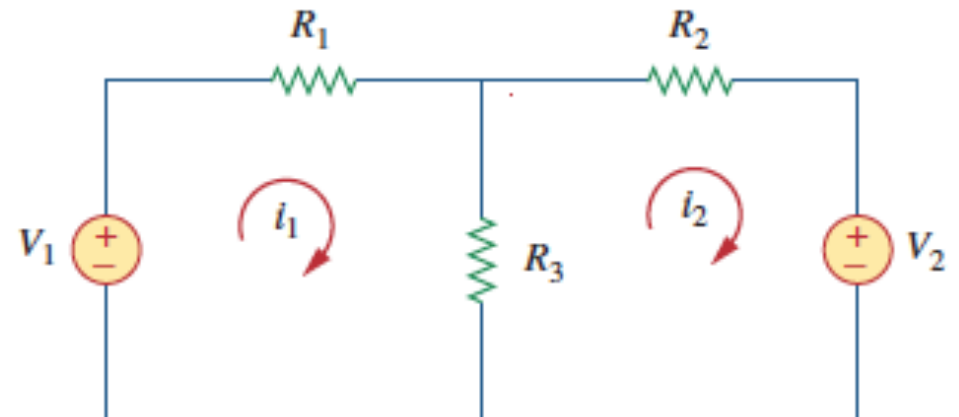
- We need a more direct approach:
 - Nodal analysis (KCL based)
 - Mesh analysis (KVL based, **NOW**)

Mesh Analysis

- Limited to “planar” circuits only



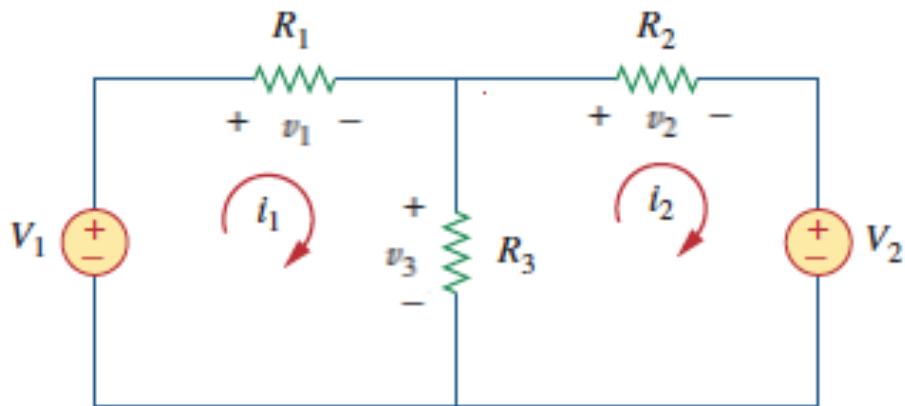
- Method – define the “mesh” currents



- Write KVL on these meshes

$$v_1 + v_3 = V_1$$

$$v_3 = v_2 + V_2$$



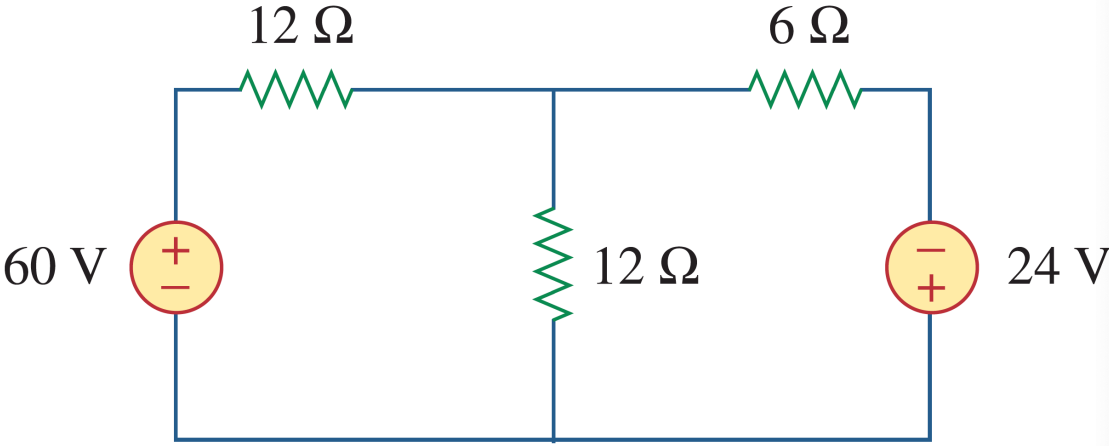
- Use Ohm's Law for voltages on resistive branches

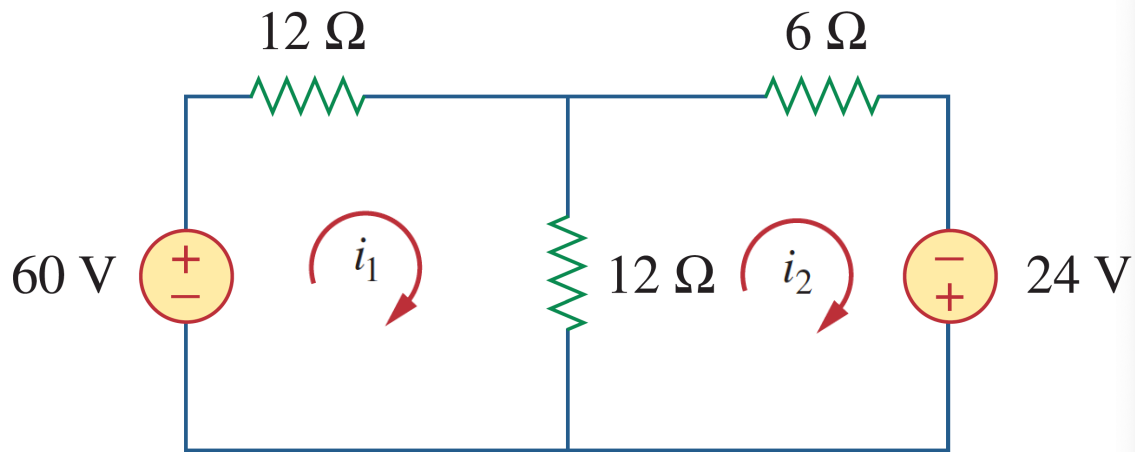
$$v = R i$$

- Careful on current directions

- Result is a set of simultaneous equations to solve

Example (details on next slide)





$$60 - 12i_1 - 12(i_1 - i_2) = 0$$

$$-12(i_2 - i_1) - 6i_2 + 24 = 0$$

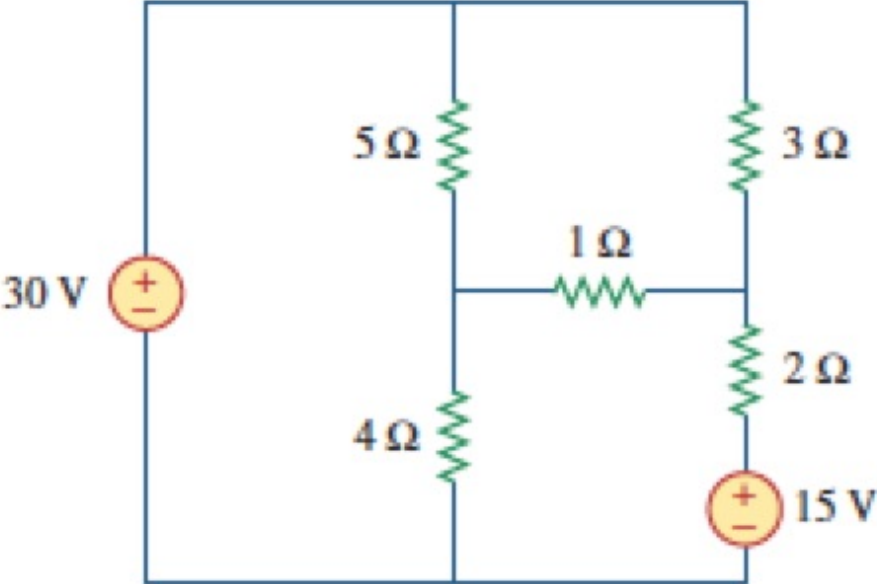
$$24i_1 - 12i_2 = 60$$

$$-12i_1 + 18i_2 = 24$$

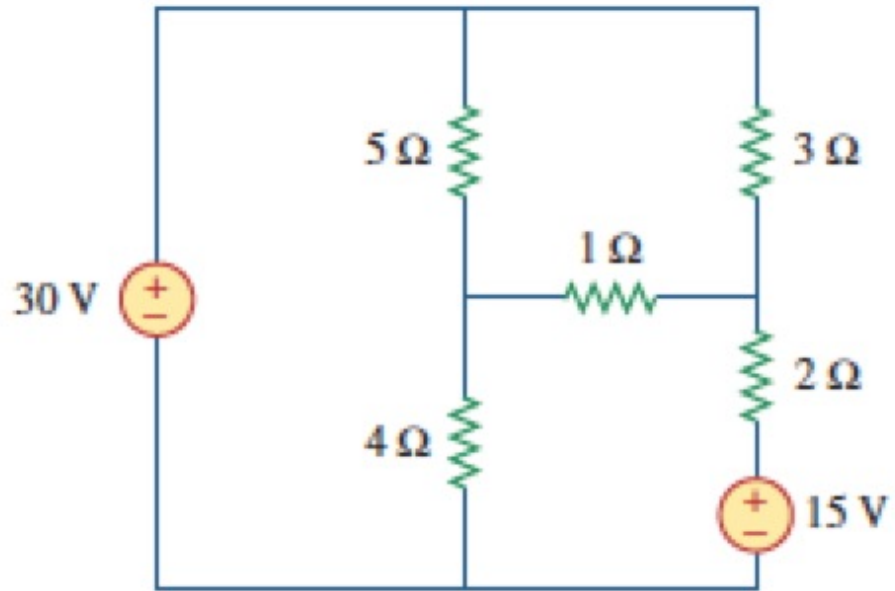
$$i_1 = \frac{\begin{vmatrix} 60 & -12 \\ 24 & 18 \end{vmatrix}}{\begin{vmatrix} 24 & -12 \\ -12 & 18 \end{vmatrix}} = \frac{1368}{288} = 4.75 \text{ amps}$$

$$i_2 = \frac{\begin{vmatrix} 24 & 60 \\ -12 & 24 \end{vmatrix}}{\begin{vmatrix} 24 & -12 \\ -12 & 18 \end{vmatrix}} = \frac{1296}{288} = 4.5 \text{ amps}$$

Example:



$$i_L = 6.26 \text{ A}, i_T = 3.69 \text{ A}, i_B = 1.96 \text{ A}$$

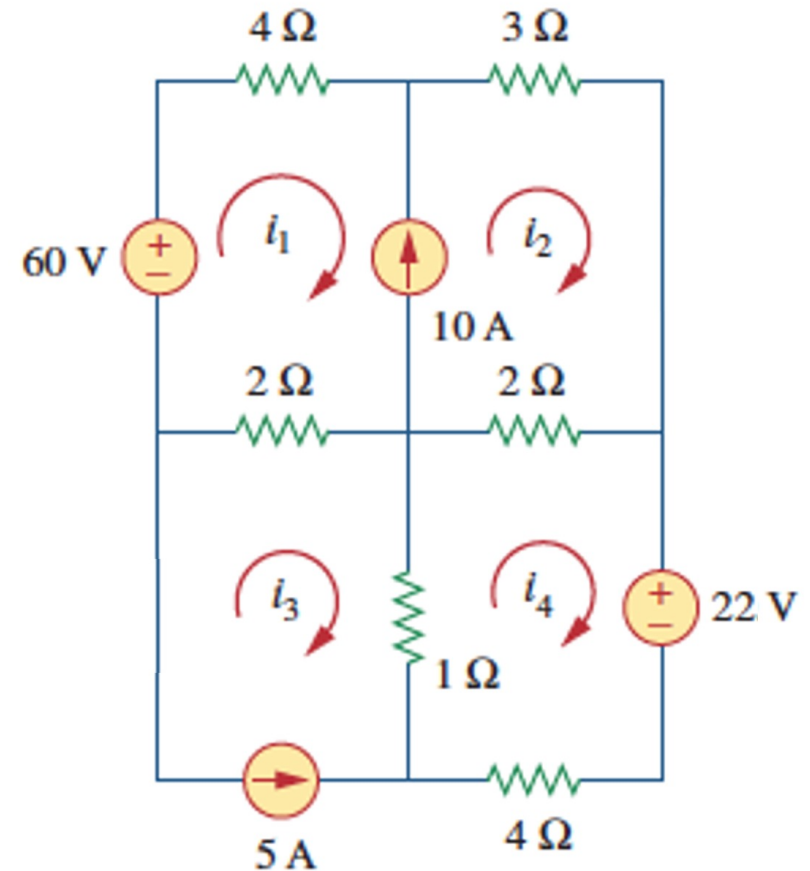


Adding Current Sources

- In only 1 mesh
 - Easy, just one less mesh to worry about

$$i_3 = -5$$

- Between meshes
 - KVL on “supermesh”

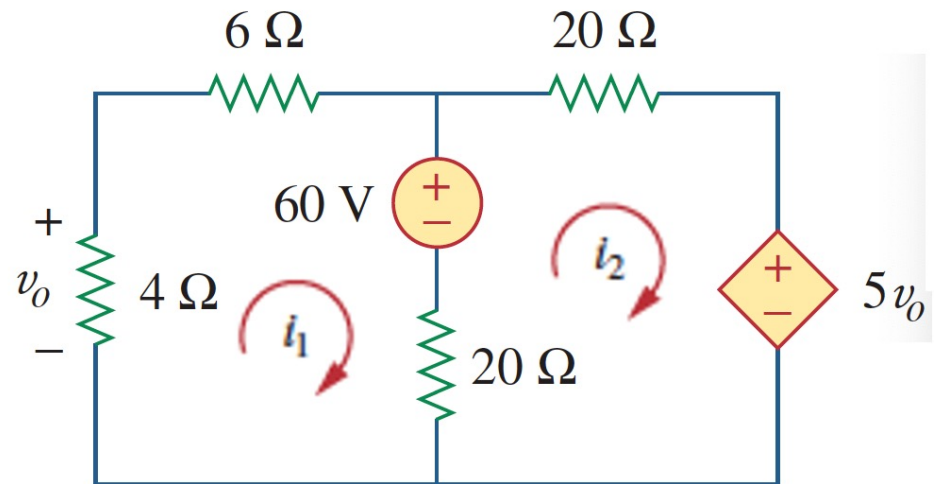


$$4i_1 + 3i_2 + 2(i_2 - i_4) + 2(i_1 - i_3) = 60$$

$$i_2 - i_1 = 10$$

Dependent Sources

- Current or voltage
 - Solve as usual
 - Extra equation for the controlling variable



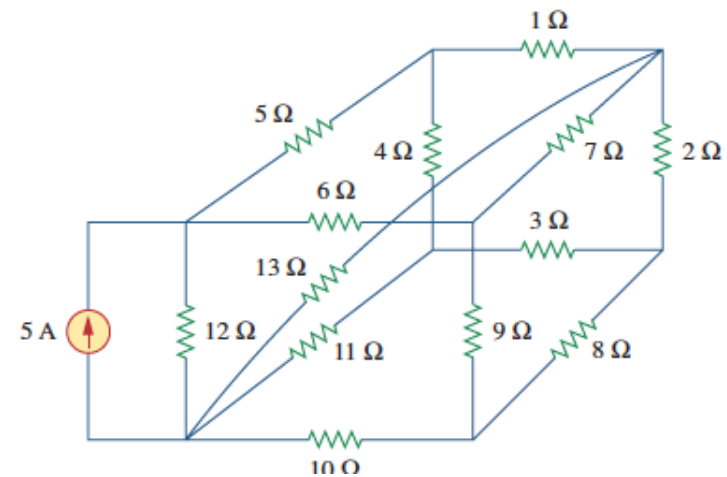
$$10 i_1 - 20 i_2 = -60$$

$$-20 i_1 + 40 i_2 = 60 - 5v_0$$

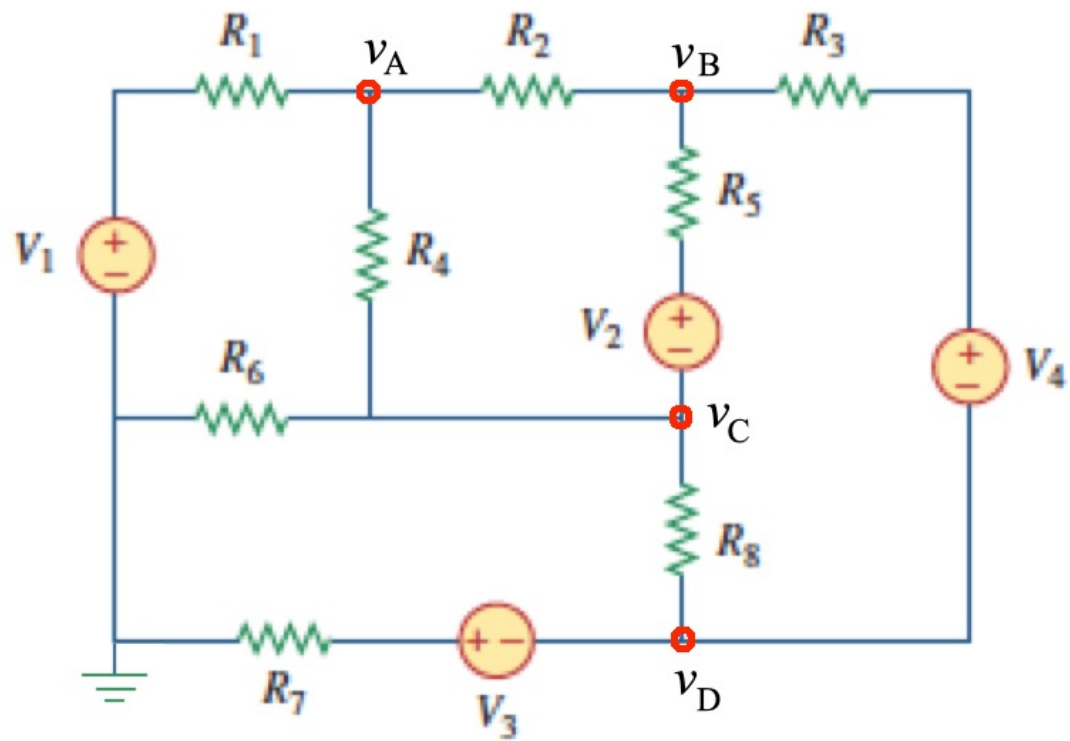
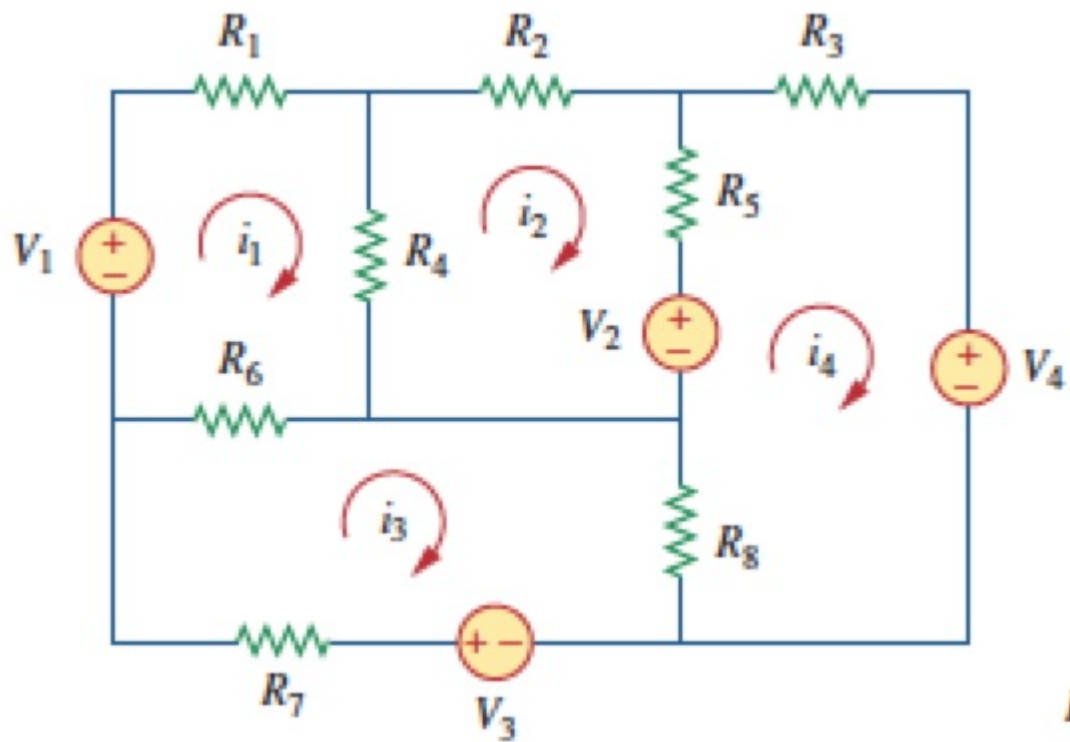
$$v_0 = -4 i_1$$

Node vs Mesh?

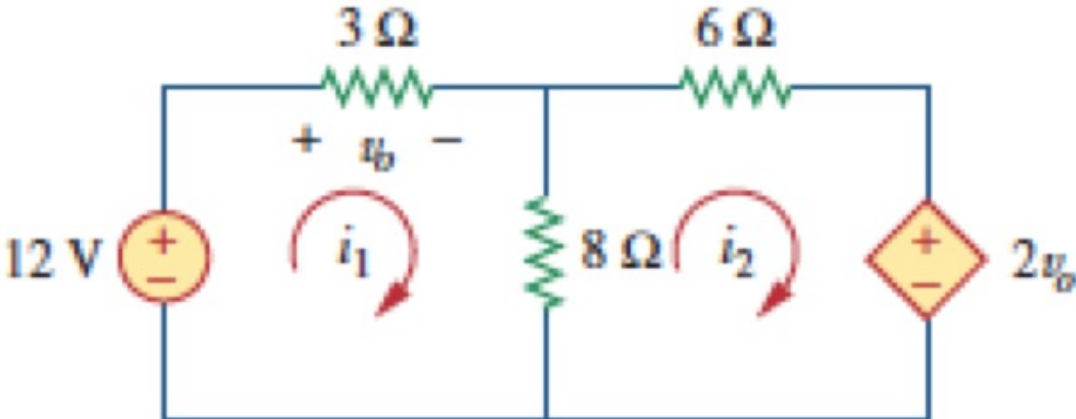
- Non-planar \rightarrow node only

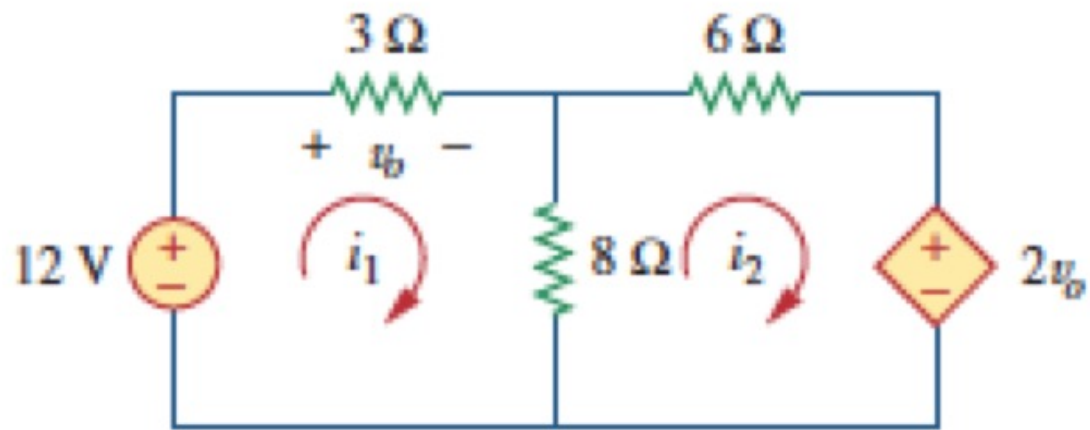


- Could count # of nodes/loops; select smaller
- Personal preference



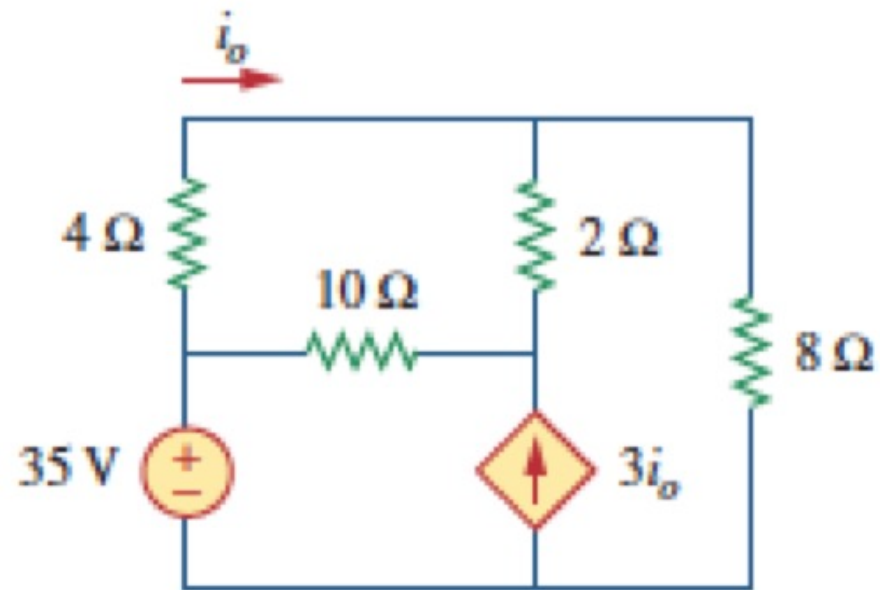
Example:

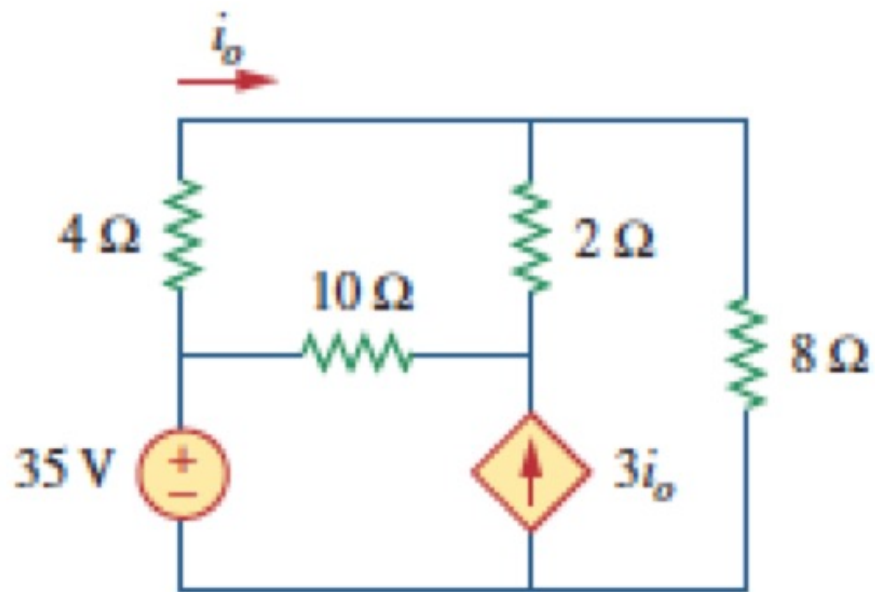




$$i_1 = 1.22 \text{ A}, i_2 = 0.174 \text{ A}$$

Example: find i_o

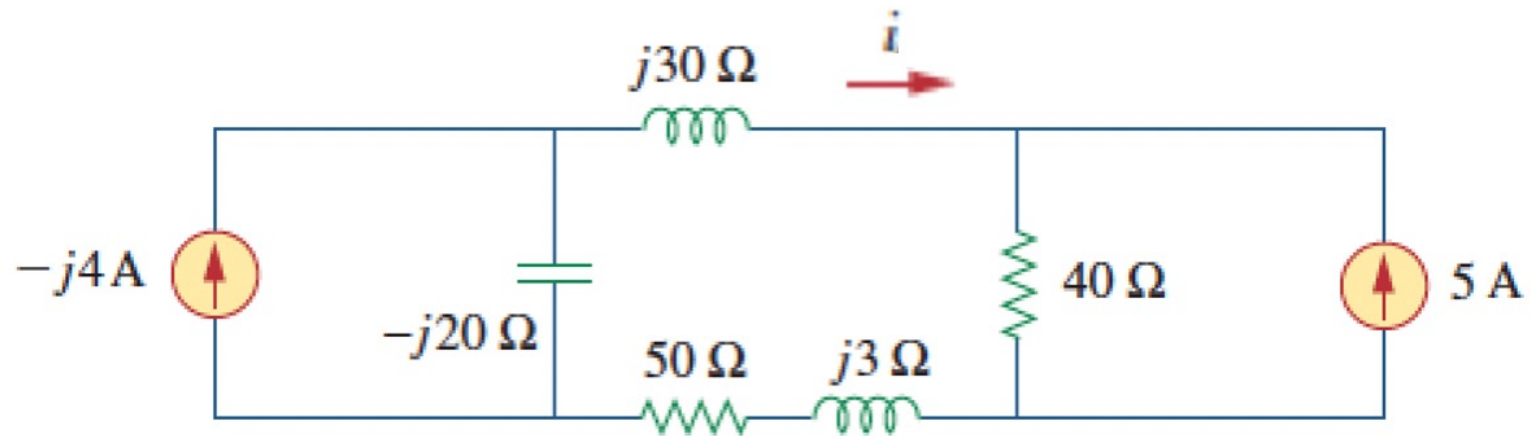




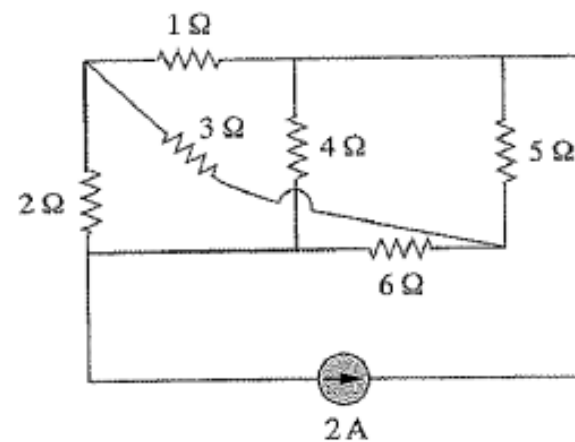
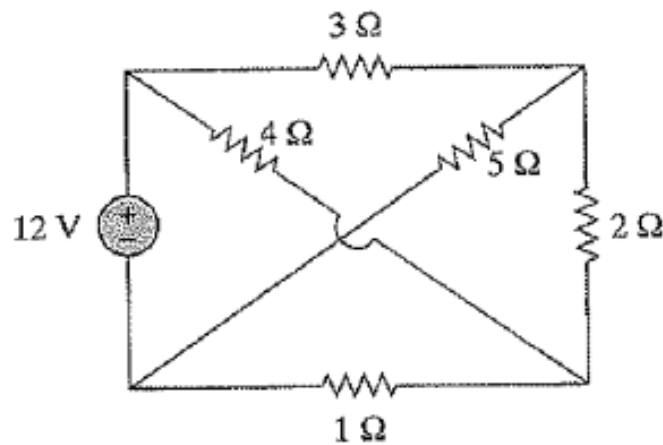
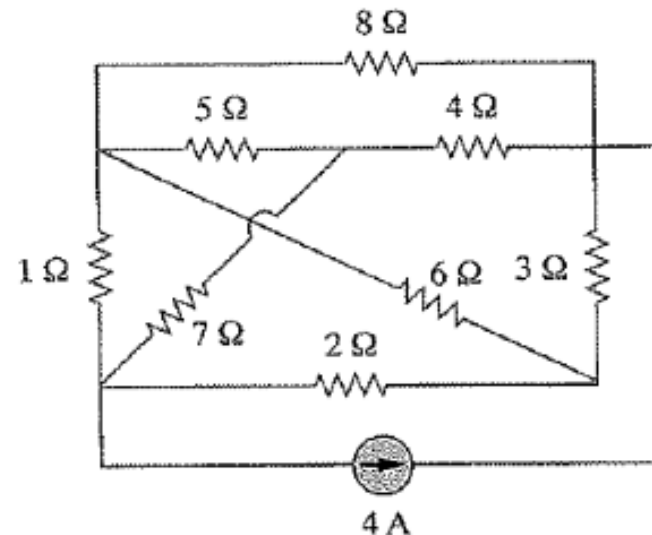
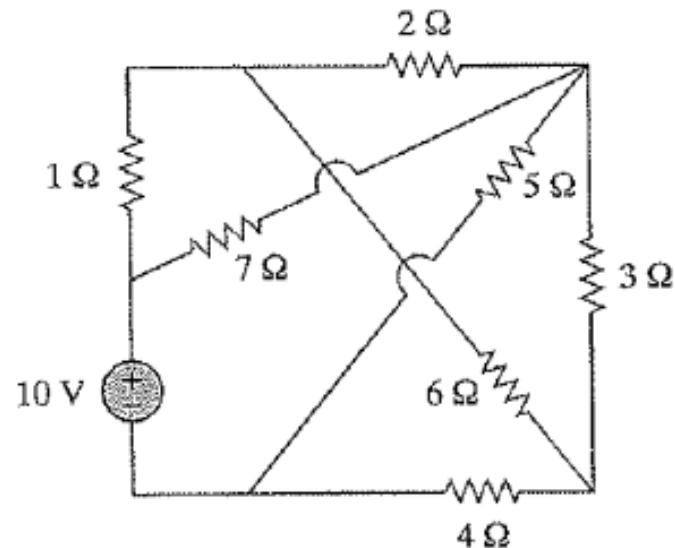
$$i_o = \frac{105}{104} A$$

Phasors, too:

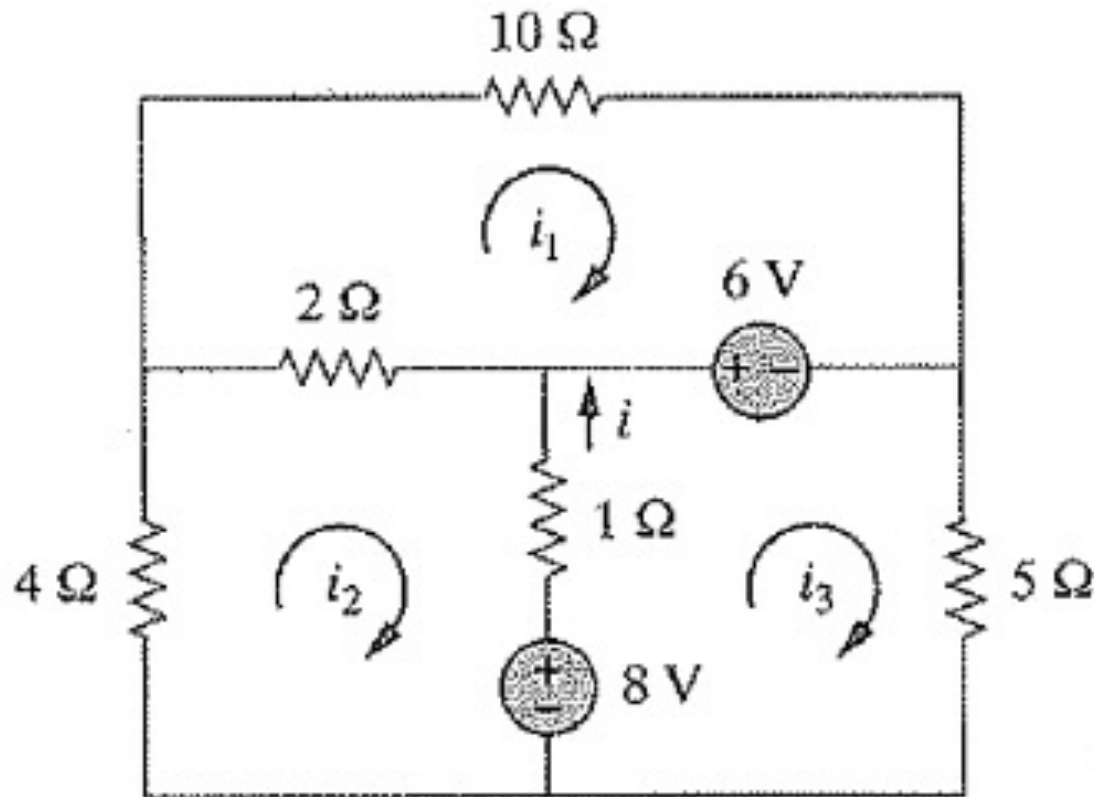
$$i = -\frac{112}{17} + \frac{j28}{17} \text{ A}$$



Practice problem: Which of these circuits are planar (i.e. would allow for mesh analysis)?



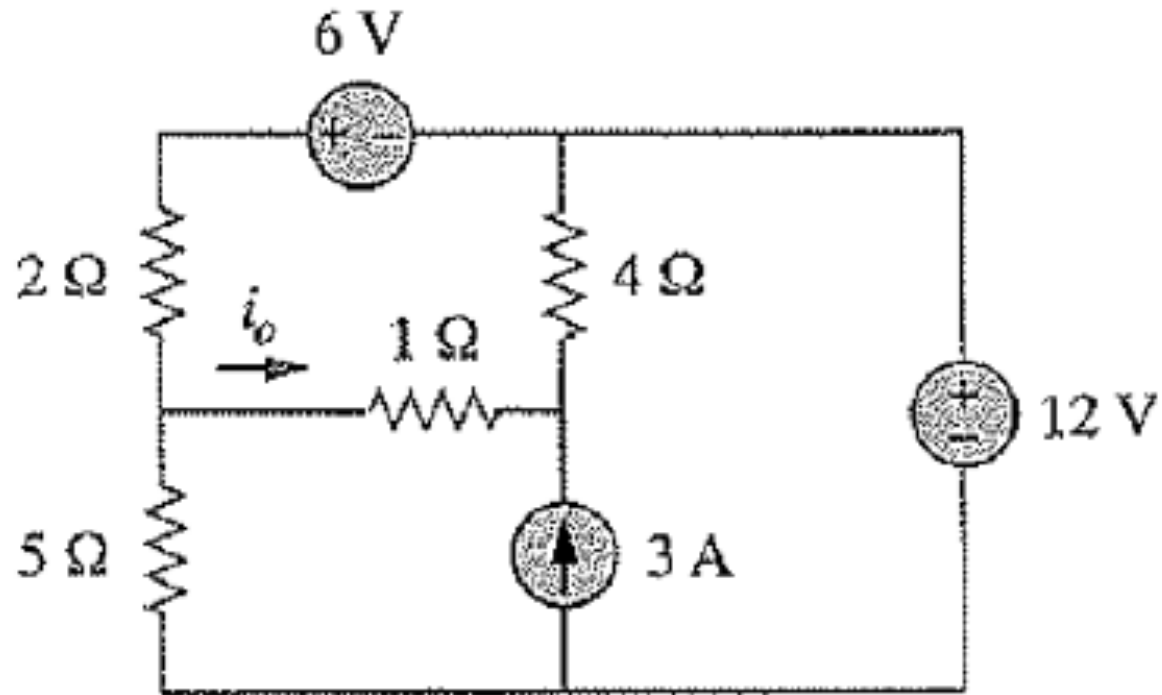
Practice problem: Find the currents i_1 , i_2 , and i_3 .



$$i_1 = \frac{77}{234} \text{ A}$$
$$i_2 = -\frac{240}{234} \text{ A}$$
$$i_3 = \frac{38}{234} \text{ A}$$

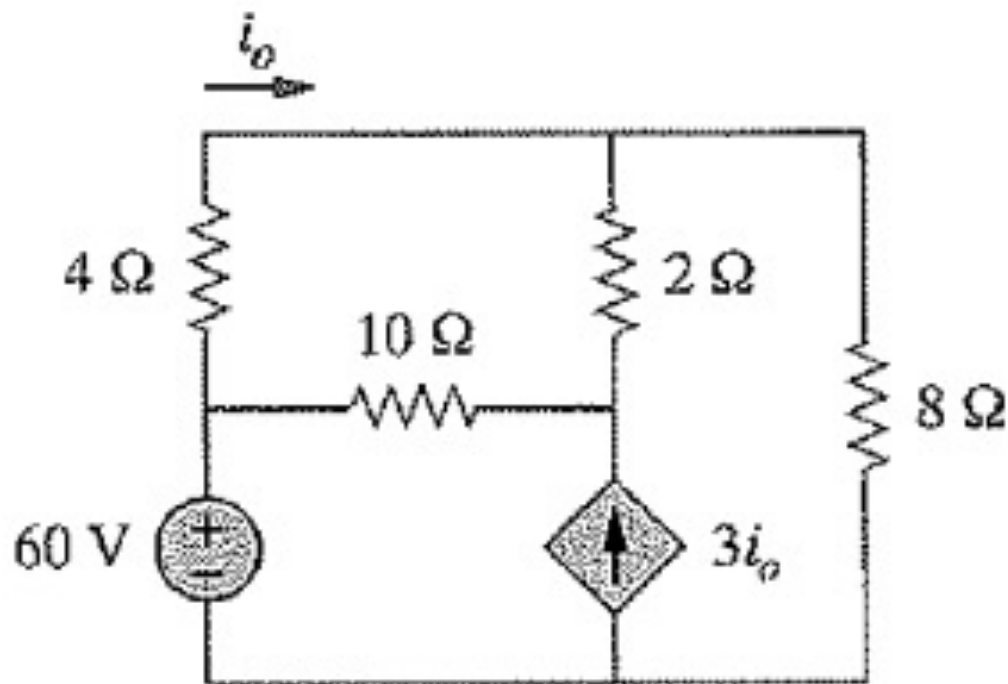
Practice problem: Find the current i_0

$$i_0 = -\frac{26}{15} \text{ A}$$

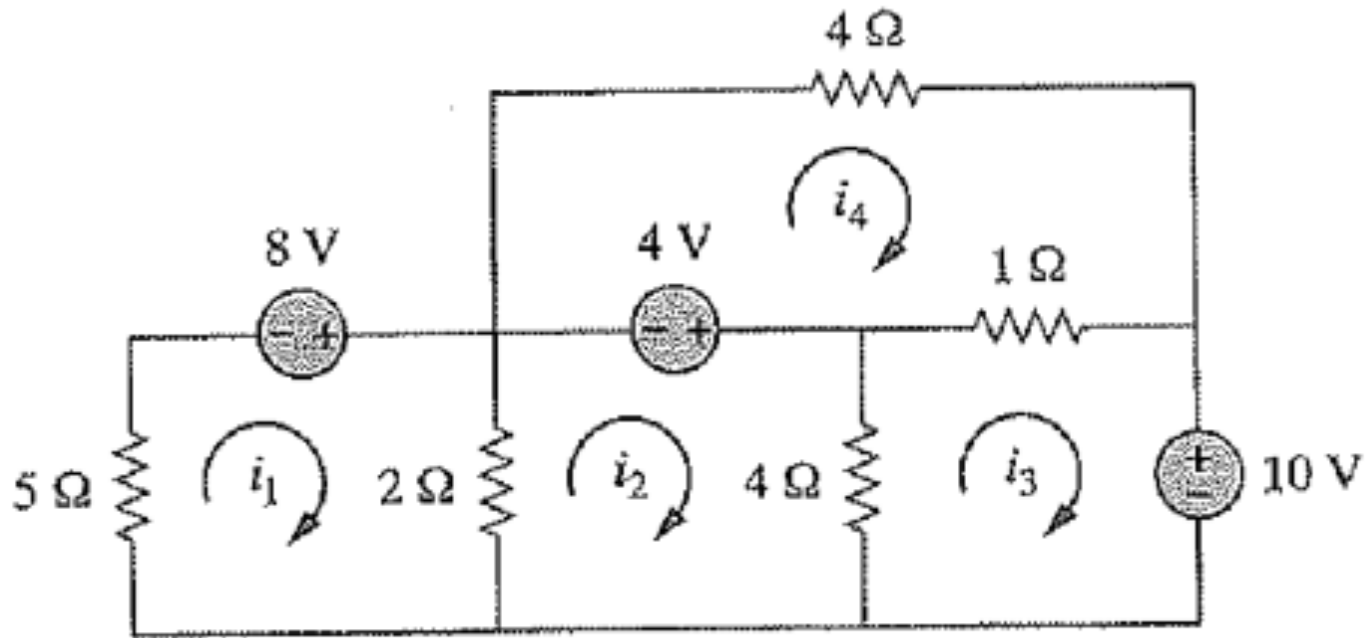


Practice problem: Find the current i_0

$$i_0 = \frac{45}{26} \text{ A}$$



Practice problem: Find the currents i_1 , i_2 , i_3 , and i_4



$$i_1 = \frac{68}{88} \text{ A}$$

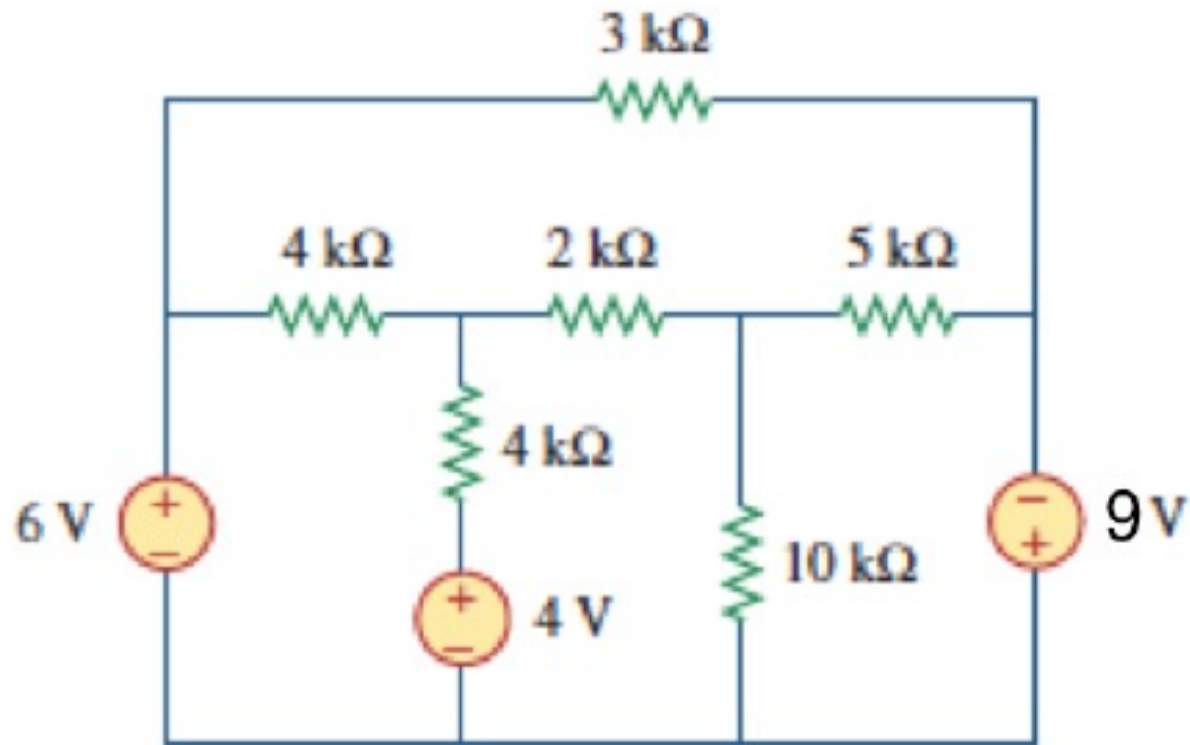
$$i_2 = -\frac{114}{88} \text{ A}$$

$$i_3 = -\frac{293}{88} \text{ A}$$

$$i_4 = -\frac{129}{88} \text{ A}$$

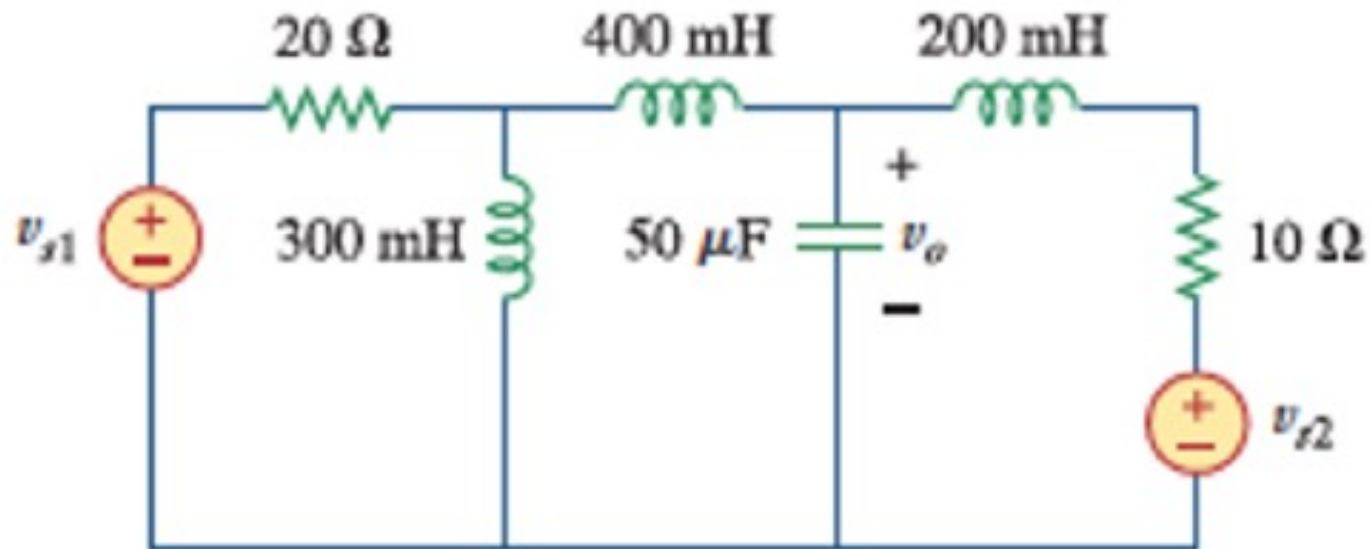
Practice problem: For the circuit below which method appears easier, mesh or node? Use your preference to find the power dissipated in the $10\text{ k}\Omega$ resistor.

$100\ \mu\text{W}$



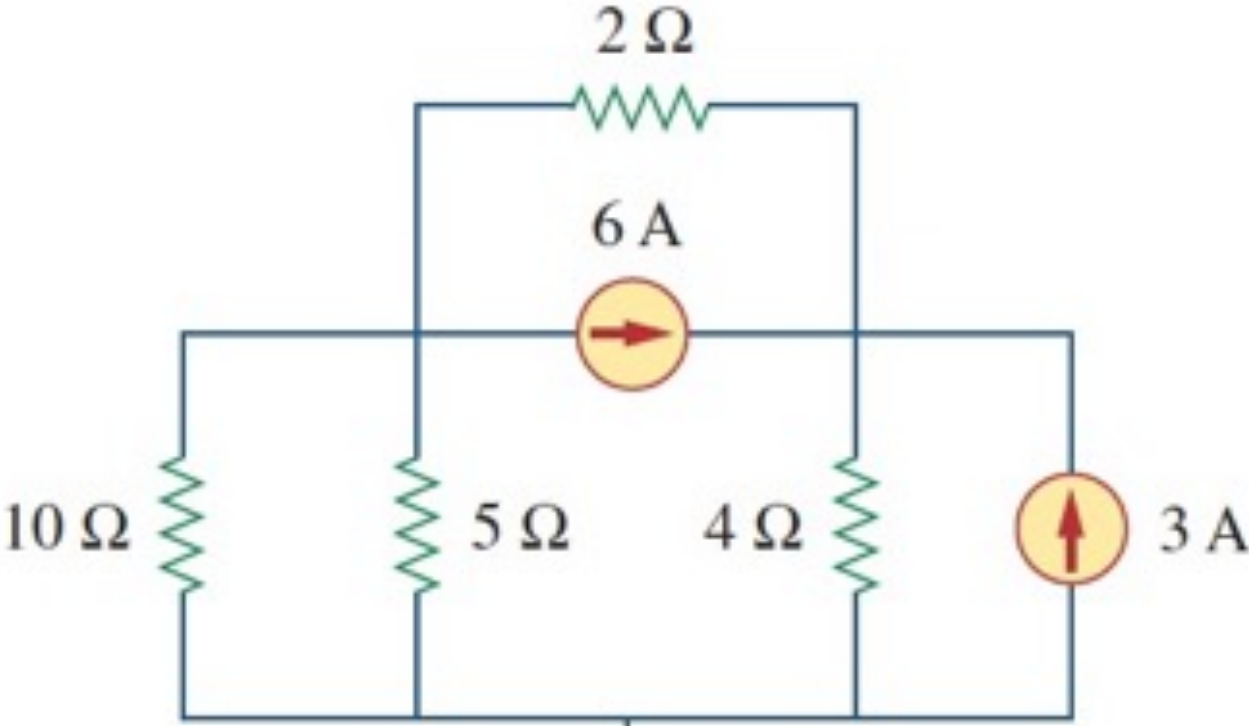
Practice problem: Find $v_o(t)$ assuming that $v_1(t) = 120 \cos(100t + 90^\circ)$ V and $v_2(t) = 80 \cos 100t$ V

$$v_o(t) = 29.9 \cos(100t + 46^\circ) \text{ V}$$



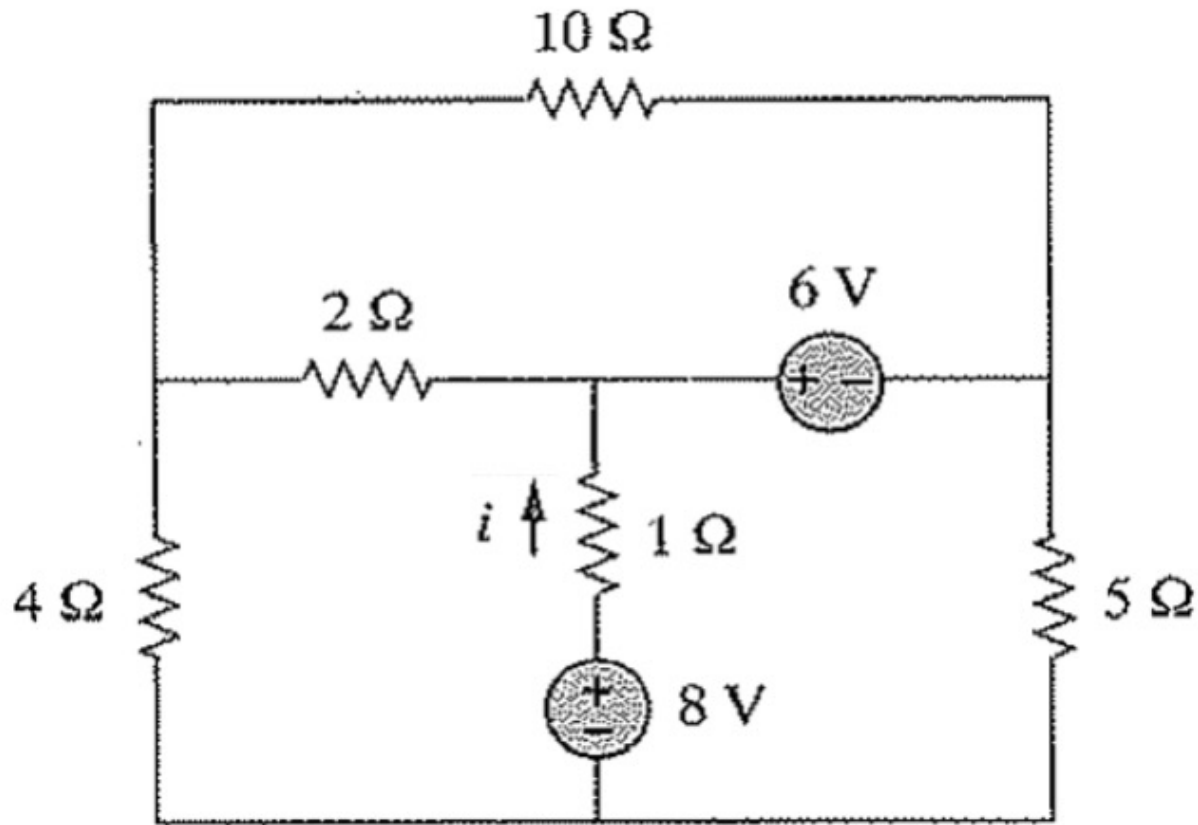
Practice problem: Find the power in the $10\ \Omega$ resistor

$0\ W$



$$i = 1.18 \text{ A}$$

Practice problem: Find i



Practice problem: Find i_0

$$i_0 = 0.4 \text{ A}$$

