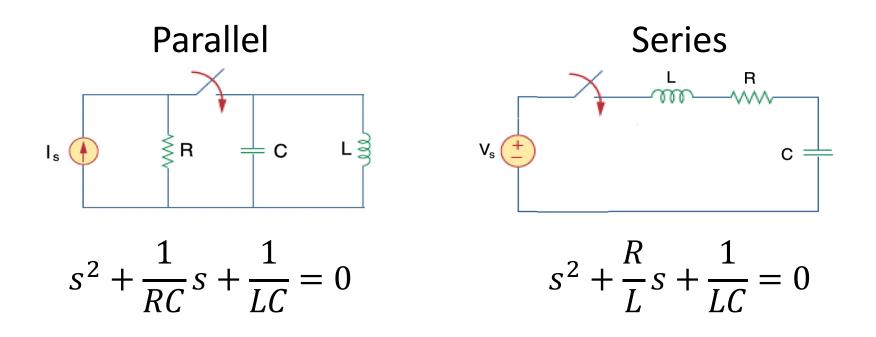
2nd Order Transients – 2

Form; more resistances; initial and final conditions

So far, for "simple" RLC circuits

 Step 1 – identify type and form characteristic polynomial



 Step 2 – based on real vs complex roots, identify form of solution

Real roots:

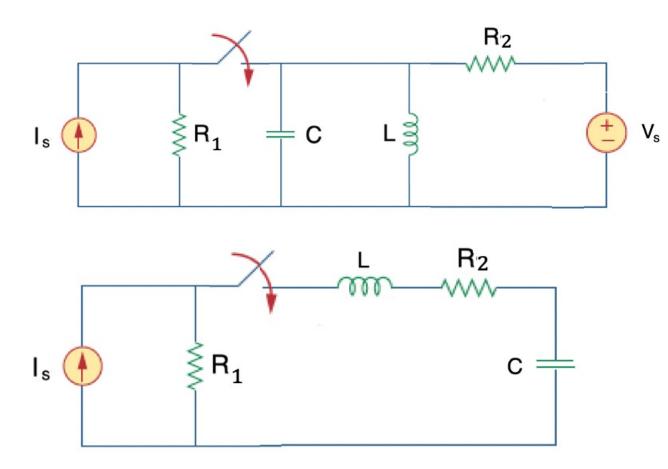
$$x(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t} + x_{\infty}$$

Complex roots:

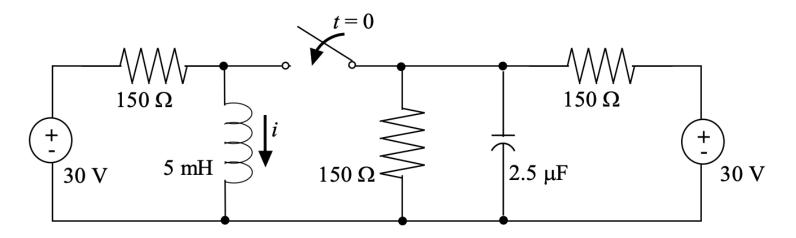
$$x(t) = B_1 e^{-\alpha t} \cos \omega_d t + B_2 e^{-\alpha t} \sin \omega_d t + x_{\infty}$$

- Step 3 use final value to evaluate x_{∞}
- Step 4 the other constants?

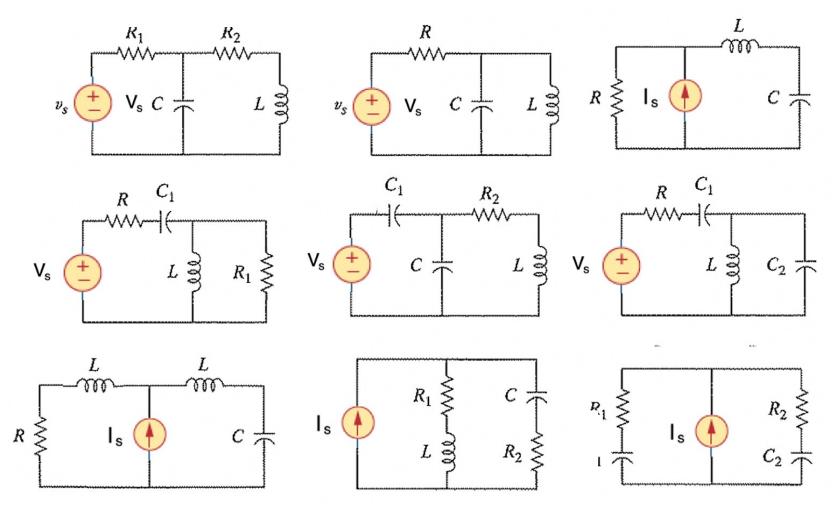
• Aside – what if we add an extra resistor?



• Or several?

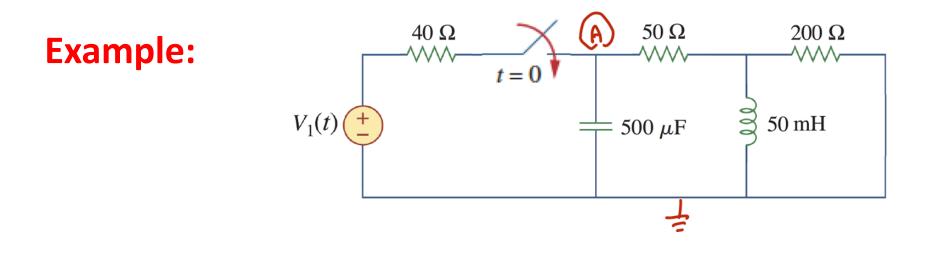


Question: Which of these circuits match our assumed 2nd order RLC circuit form? If yes, which form, series or parallel?



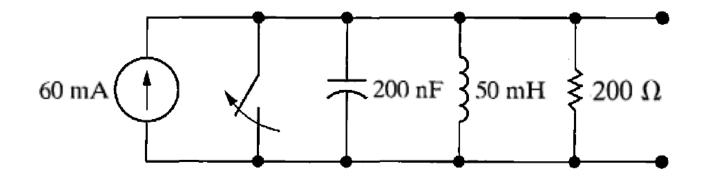
Initial and Final Conditions

- Just like the 1st order case:
 - From a DC analysis based on "open" or "short" models for C and L both before and after the switch event
 - Before switching event yields initial values
 - After switching event yields final values

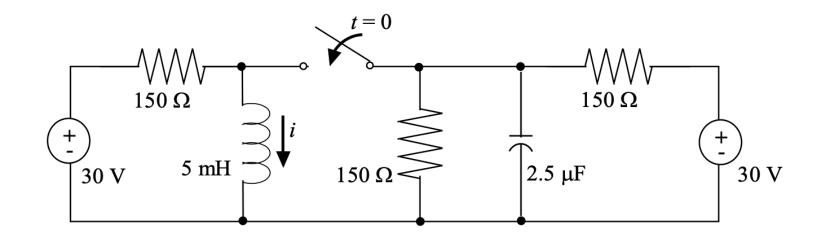


$$A(t) = a_0 + a_1 e^{-94.3t} + a_2 e^{-764t}$$

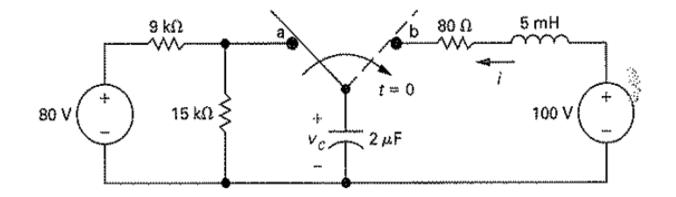
• A(0) = 0• $A(\infty) = \frac{5}{9}V_1$ $a_0 = \frac{5}{9}V_1$ $a_0 + a_1 + a_2 = 0$ **Example:** Find the initial/final conditions



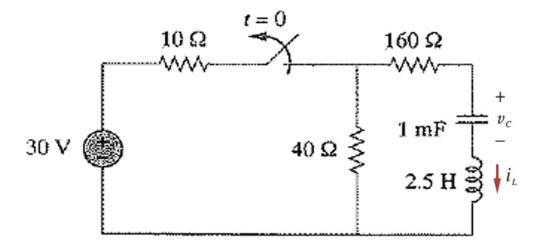
Example: Find the initial/final conditions

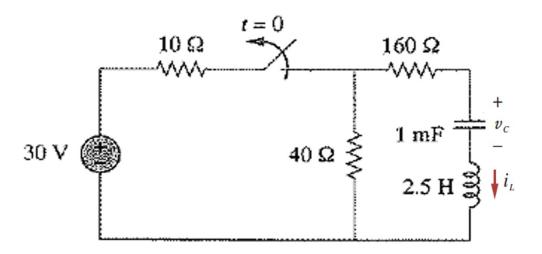


Example: Find the initial/final conditions



Practice problem: Find the form of solution and the initial/final conditions





$$i_L(0) = 0 A$$

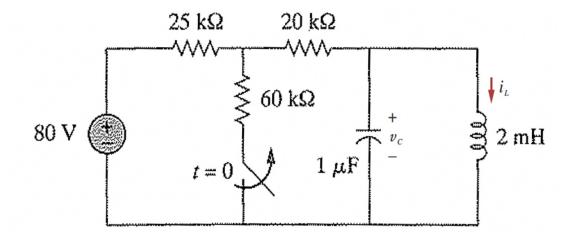
$$i_L(\infty) = 0 A$$

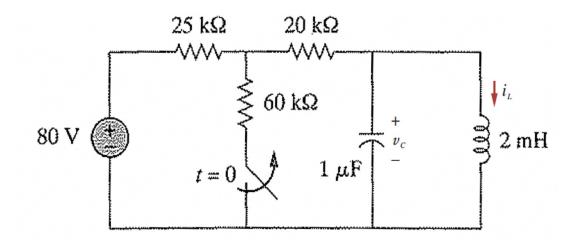
$$v_C(0) = 24 V$$

$$v_C(\infty) = 0V$$

$$x(t) = A_1 e^{-5.36t} + A_2 e^{-74.6t} + x_{\infty}$$

Practice problem: Find the form of solution and the initial/final conditions





$$i_L(0) = 1.5 A$$

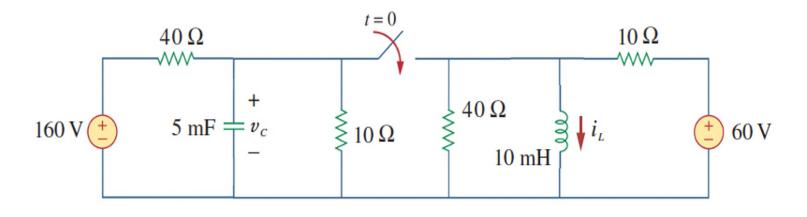
$$i_L(\infty) = \frac{16}{9} A$$

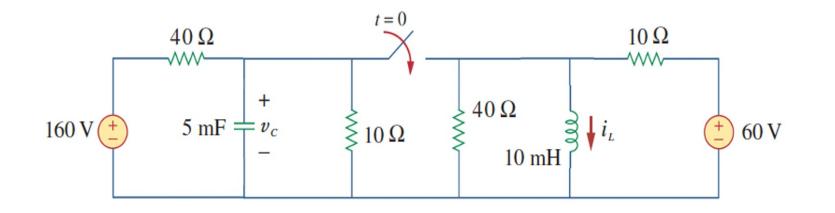
$$+ x_{\infty} \qquad v_C(0) = 0 V$$

$$v_C(\infty) = 0 V$$

 $x(t) = B_1 e^{-11.1t} \cos 22361t + B_2 e^{-11.1t} \sin 22361t + x_{\infty}$

Practice problem: Find the form of solution and the initial/final conditions





 $x(t) = B_1 e^{-25t} \cos 139t + B_2 e^{-25t} \sin 139t + x_{\infty}$

 $i_L(0) = 6 A$ $i_L(\infty) = 10 A$ $v_C(0) = 32 V$ $v_C(\infty) = 0 V$