# Theorems – 1

linearity & superposition; transformations

# **Linearity & Superposition**

 <u>Linearity</u>: for a single "input" (voltage or current), the "output" (voltage or current) is proportional to that input

$$v_o = k v_s$$

• What about multiple "input" sources?



• Analyzing



$$\frac{v_o - V}{R_1} + \frac{v_o}{R_2} - I = 0$$

or

$$v_o = \frac{R_1 R_2}{R_1 + R_2} I + \frac{R_2}{R_1 + R_2} V$$

• And the idea extends to multiple "input" sources

$$v_o = k_1 v_{s1} + k_2 v_{s2}$$

"Superposition"

• We can exploit this idea to decompose problems:



# **Example:** find *i*



i = 1.67 A

## **Phasor example:** note differet frequencies



 $v(t) = 10\cos(t - 90^\circ) + 1.2\cos(2t + 127^\circ)V$ 

# **Source Transformations**



- These two sub-circuits are equivalent at the terminals a, biff  $v_s = R I_s$ 

- Utility: simplify circuit for quick analysis



**Example:** find *i* (convert to just one node)



1.67 *A* 



 $i_x(t) = 10\cos(2t + 174^\circ) V$ 

• To find *i*, recall series/parallel combining:





 Can combine transformations with series/parallel combining









# **Example:** find *i* (convert to parallel current sources and then current division)



## **Example from above:** find *i* (use current division)



#### 1.67 A

# **Example:** find $i_{\Delta}$



$$i_{\Delta} = \frac{223}{130} A$$

# **Example:** find *i*



 $i(t) = 8.94 \cos(200t + 56.6^\circ) A$ 

**Practice problem:** find  $v_o$  and  $i_o$ 



$$v_o = 8 V, \qquad i_o = \frac{2}{3} A$$

## **Practice problem:** find *i*<sub>o</sub>





 $i_o = 1.79 A$ 

# **Practice problem:** find *i*<sub>o</sub>



# **Practice problem:** find $v_o$

$$v_o = -11 V$$



# **Practice problem:** find $v_{\chi}$ if = $v_s(t) = 50 \cos(2t + 90^\circ) V$ and $i_s(t) = 12 \cos(2t + 10^\circ) A$

 $i_{x} \bullet 16 \Omega \stackrel{20 \Omega}{\stackrel{5 H}{\stackrel{0}{\underset{}}}_{v_{x}} \circ \underbrace{}^{t} v_{x} \circ \underbrace{}^{t} v_{x}$ 

 $v_x(t) = 129\cos(2t + 28.76^\circ)V$