

Phasors – 8

more AC power; start design

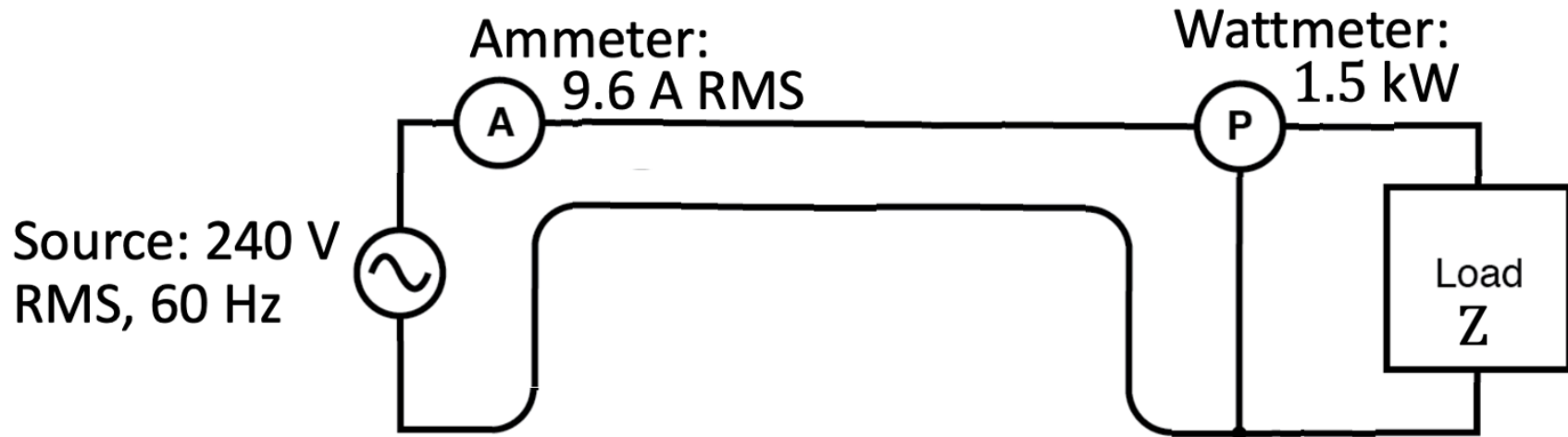
Improving AC Power Delivery

- Real average power is

$$P = \frac{VI}{2} \cos \theta = V_{RMS} I_{RMS} \cos \theta$$

- The goal is to get θ close to 0 (equivalently, S close to real
 - Load close to resistive

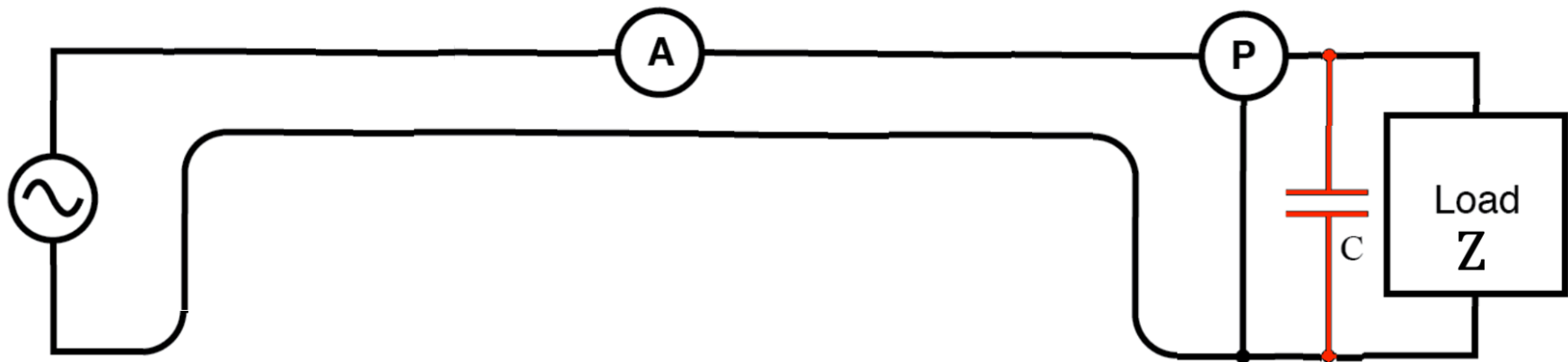
A Typical Example – Power Distribution



- Load Apparent power is

$$P = V_{RMS} I_{RMS} = 240 * 9.6 = 2.3 \text{ kVA}$$

- Real power = 1.5 kW, so power factor = $\frac{1.5}{2.3} = 0.65$
- Can we improve this? e.g. get current below 7 amps?



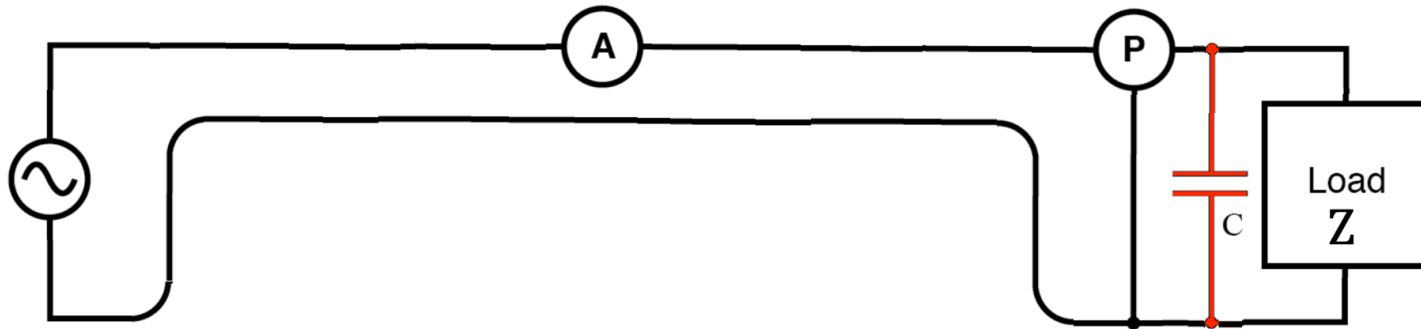
- Since a typical load is inductive, using the power factor value of 0.65 then the model is likely to be:

$$|Z| = \frac{240}{9.6} = 25 \Omega$$

$$\begin{aligned} Z &= R + jX \\ &= 16.25 + j19 \end{aligned}$$

- Try to improve matters with a shunt capacitor, C , so

$$Z_{new} = Z \parallel \frac{1}{j\omega C}$$

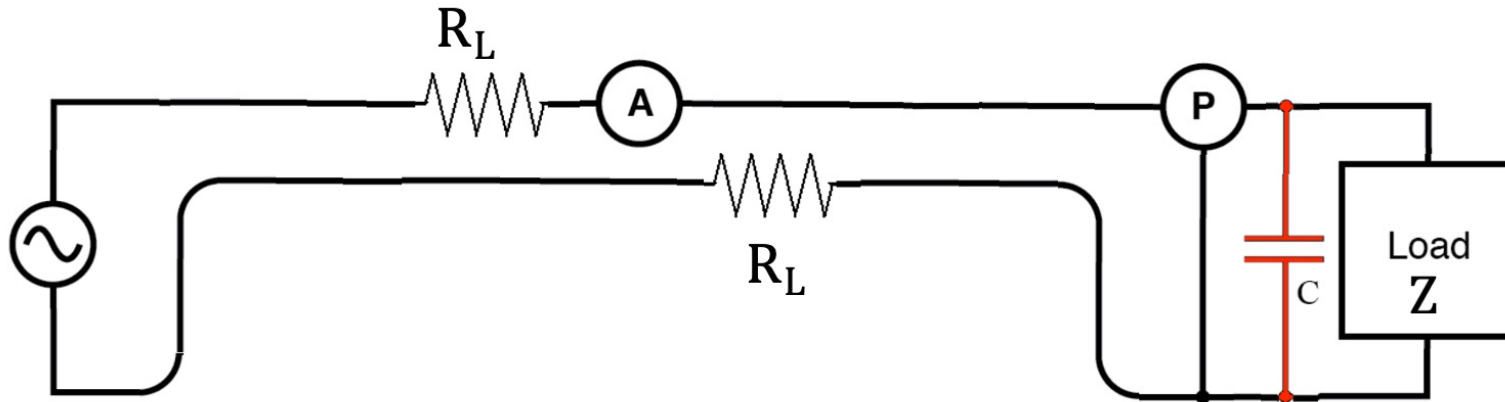


$$Z_{new} = Z \parallel \frac{1}{j\omega C} = \frac{Z \frac{1}{j\omega C}}{Z + \frac{1}{j\omega C}} = \dots$$

$$= \frac{R(1 - \omega CX) + \omega RCX}{(1 - \omega CX)^2 + \omega^2 R^2 C^2} + j \frac{X(1 - \omega CX) - \omega R^2 C}{(1 - \omega CX)^2 + \omega^2 R^2 C^2}$$

- Want Z_{new} to be real for best performance $\rightarrow C = 80.6 \mu F$
 - $Z_{new} = 38.46 \Omega$ and now ammeter reads 6.24 A

Why this really matters: line resistance

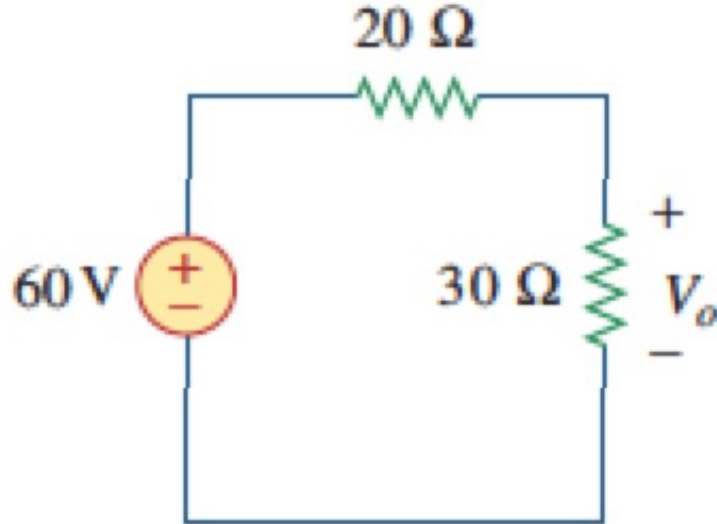


Shunt C yields higher voltage at the load and less heat in the wires

	$R_L = 0$	$R_L = 0.1 \Omega$	$R_L = 0.1 \Omega \quad C = 80.6 \mu F$
Z_L	$16.25 + j19 \Omega$	$16.25 + j19 \Omega$	38.46Ω
I_L	9.6 A	9.55 A	6.24 A
V_L	240 V	238 V	239 V
P_{Load}	1500 W	1480 W	1500 W
P_{Line}	0	18.2 W	7.79 W

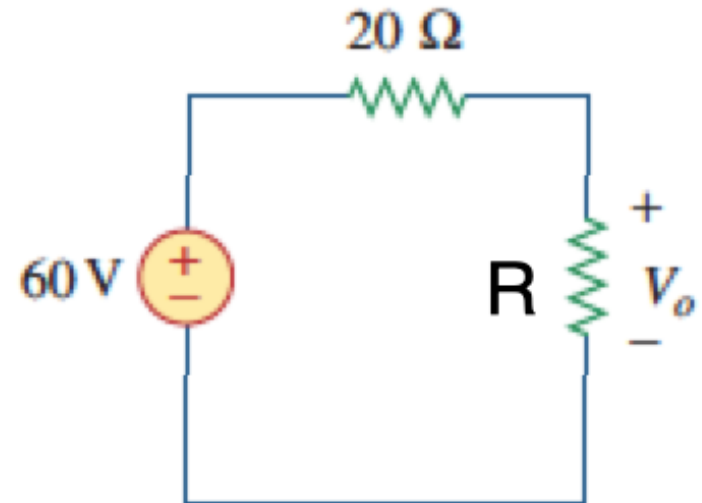
Analysis vs Design

- Voltage division **analysis** yields



$$V_o = \frac{30}{20+30} 60 = 36 \text{ volts}$$

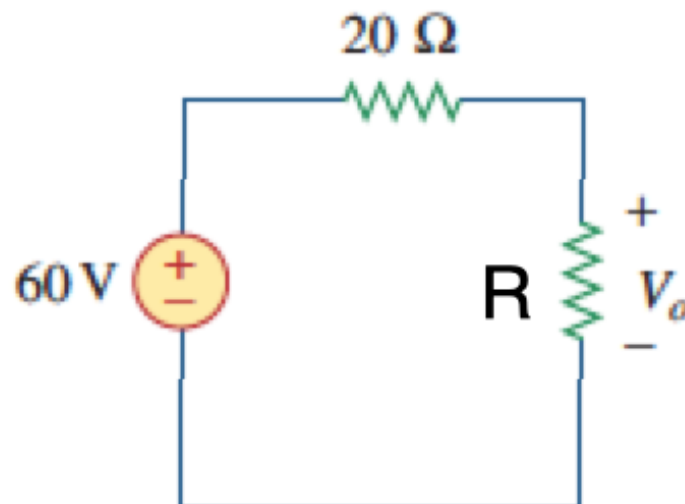
- **Design**: How do we choose R for $V_o = 10$ volts? And is this even possible?



- Solving :

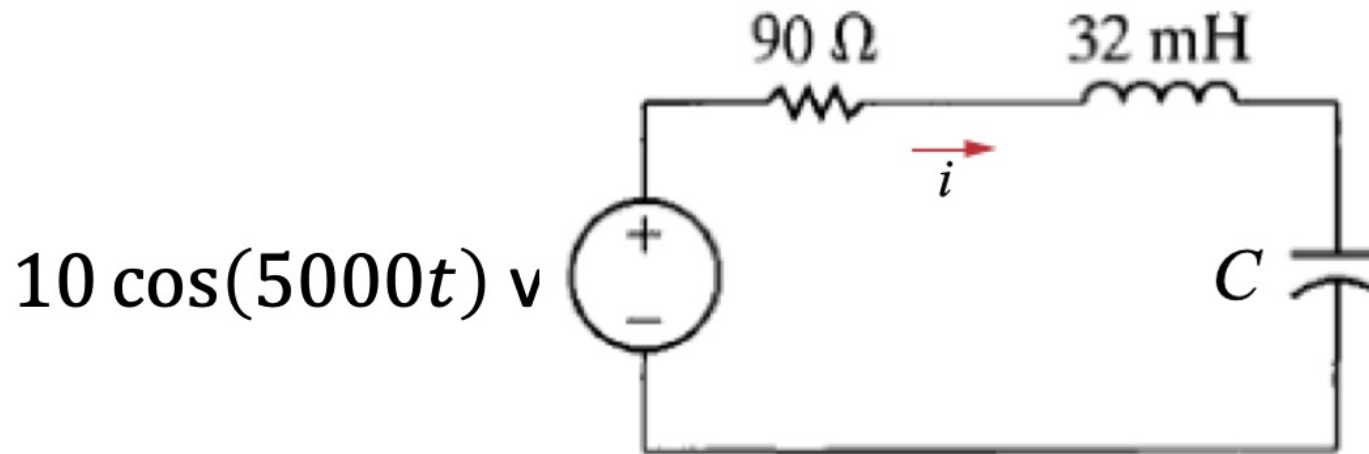
$$V_o = \frac{R}{20 + R} 60 \quad \Rightarrow \quad R = \frac{20V_o}{60 - V_o}$$

- One solution if $0 < V_o < 60$
- None otherwise



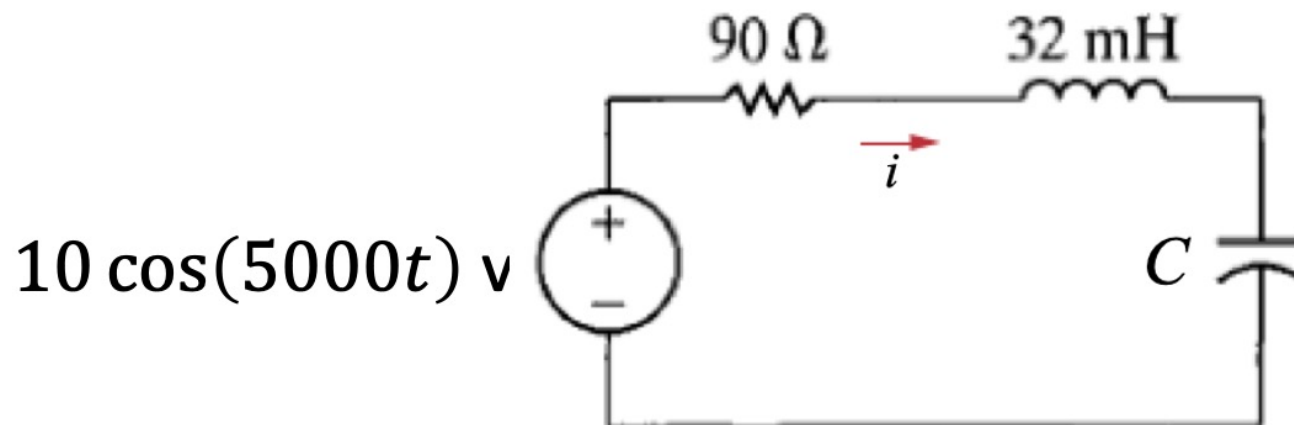
Phasor Circuit Design

- Choose components to achieve a certain goal.
- Example:



- Can you choose a capacitor C so that the steady state current i has a phase angle of -45° relative to the source? If so, what is the current's amplitude?

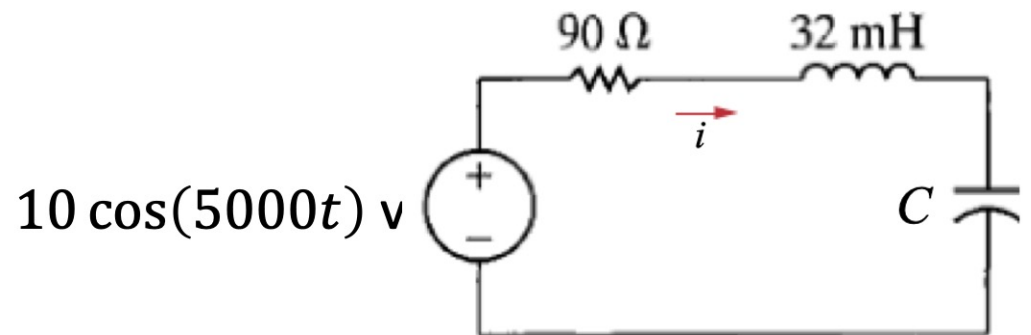
- Considerations:
 - Is the request even possible? How many degrees of freedom do you have versus the number of quantitative goals? Is more than one solution possible?
 - For our example, what range of angles is even possible?



```

om = 5000;
R = 90;
L = 32e-3;
ZL = 1j*om*L;
C = logspace(-9,-1,1000);
ZC = 1./(1j*om*C);
I = 10./(R+ZL+ZC);

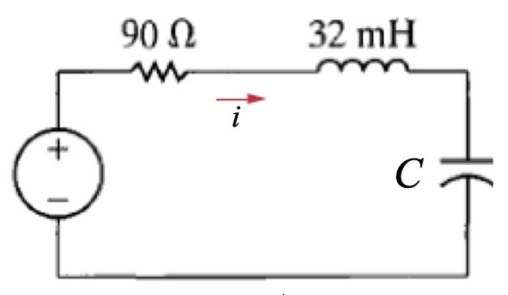
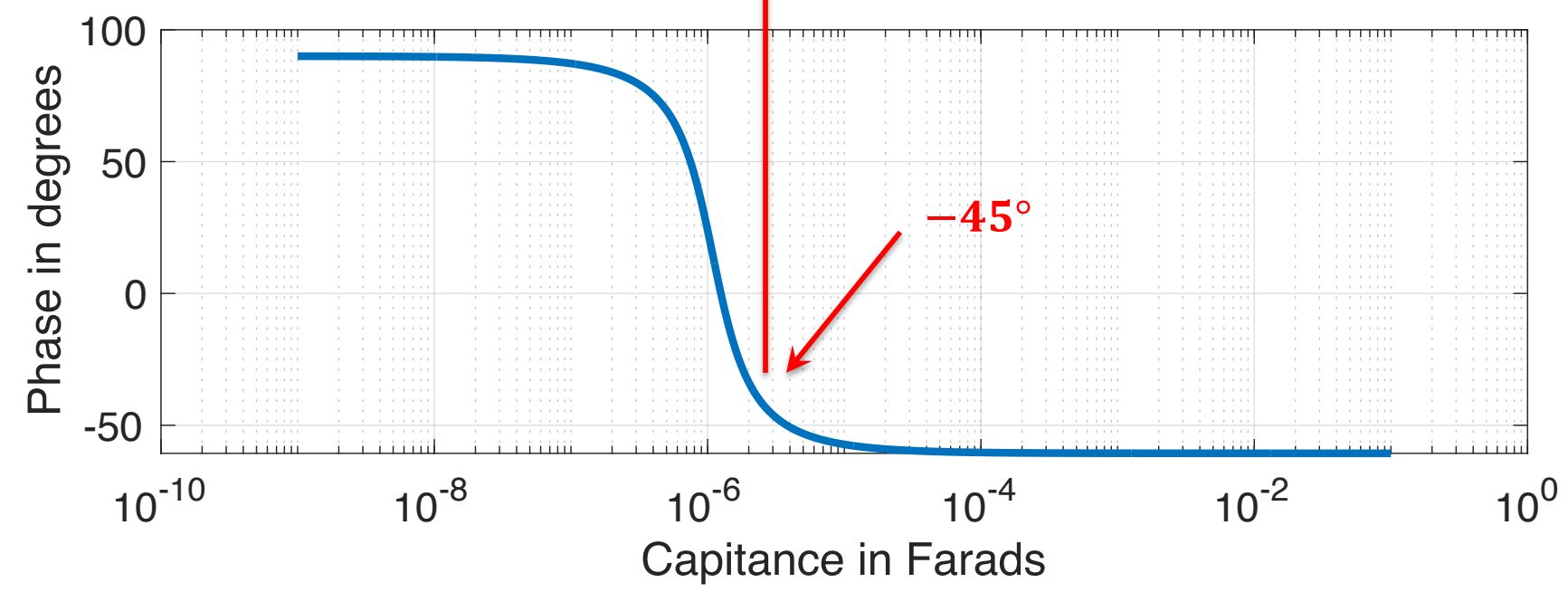
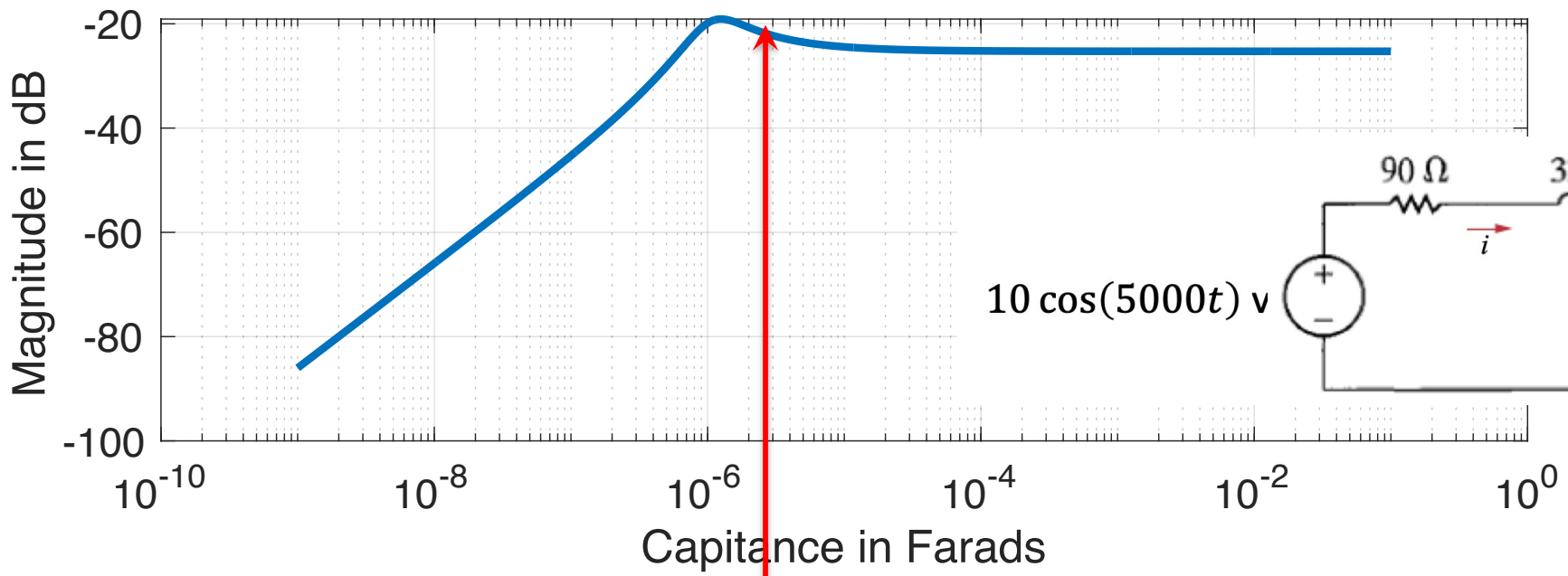
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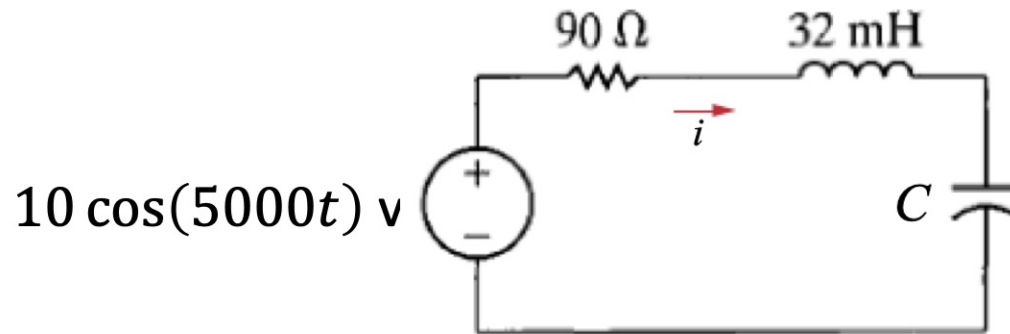
```

subplot(211)
semilogx(C,20*log10(abs(I)), 'linewidth',3)
xlabel('Capitance in Farads')
ylabel('Magnitude in dB')
set(gca, 'fontsize',16)
grid on
subplot(212)
semilogx(C,180/pi*angle(I), 'linewidth',3)
xlabel('Capitance in Farads')
ylabel('Phase in degrees')
set(gca, 'fontsize',16)
grid on

```



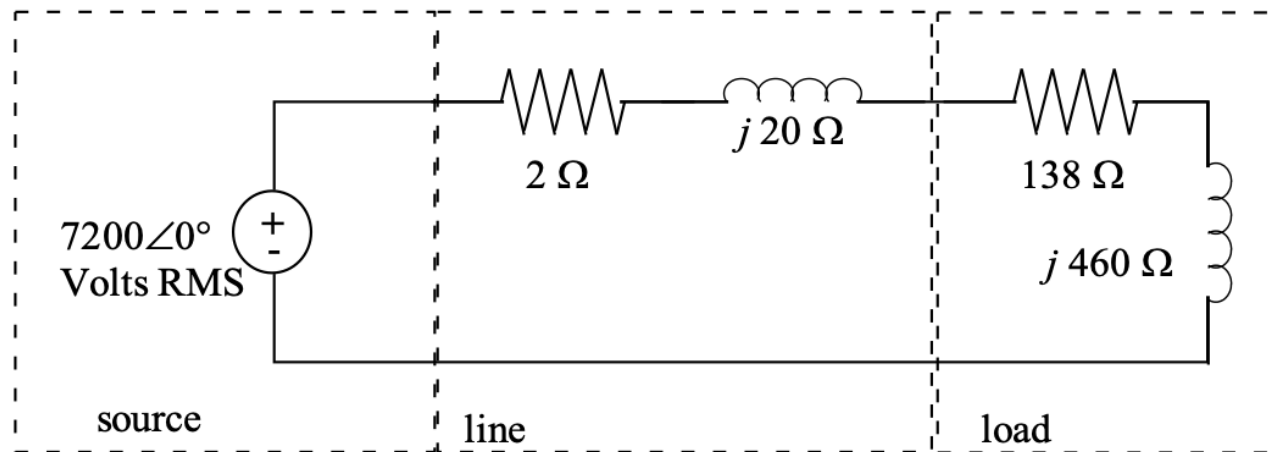
Let's actually solve for C and the current's amplitude



2.86 μF ; 78.6 mA

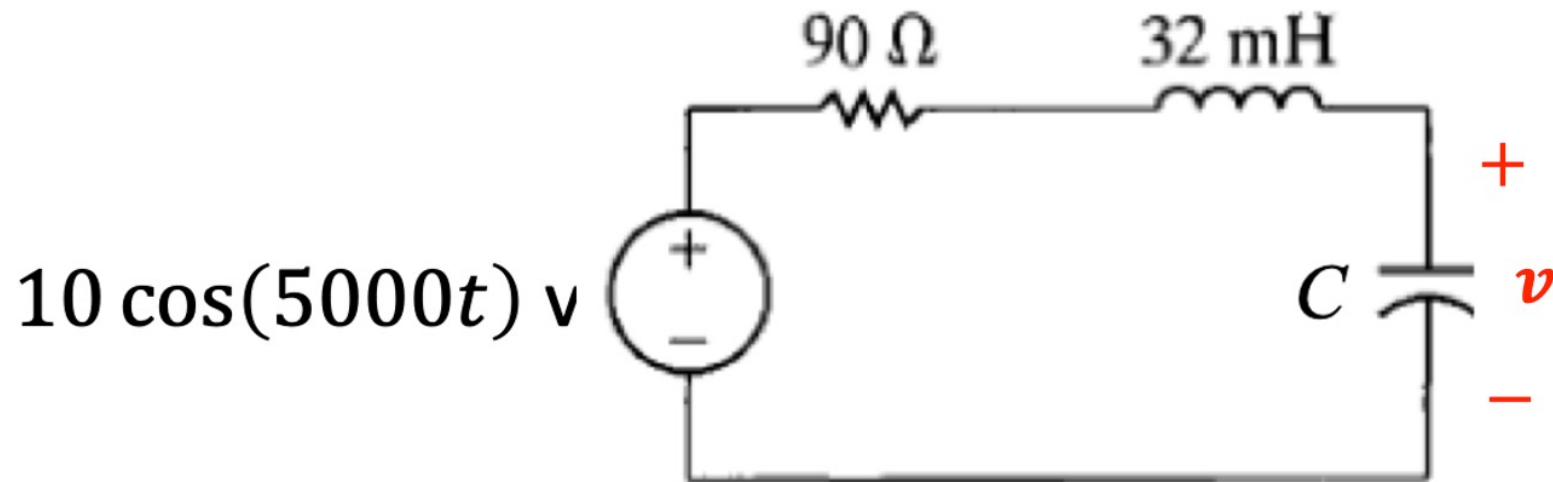
Practice problem:

- Find the average power dissipated by the line
- Find the shunt capacitance to make the load appear purely resistive
- Find the load resistance resulting from this shunt capacitance
- Find the average power dissipated by the line with the shunt capacitor installed



$207\ W; -501\ \Omega; 1.67\ k\Omega; 18.6\ W$

Practice problem: for the same circuit, Can you choose a capacitor C so that its steady state voltage v has a phase angle of -45° relative to the source ?



0.118 nF