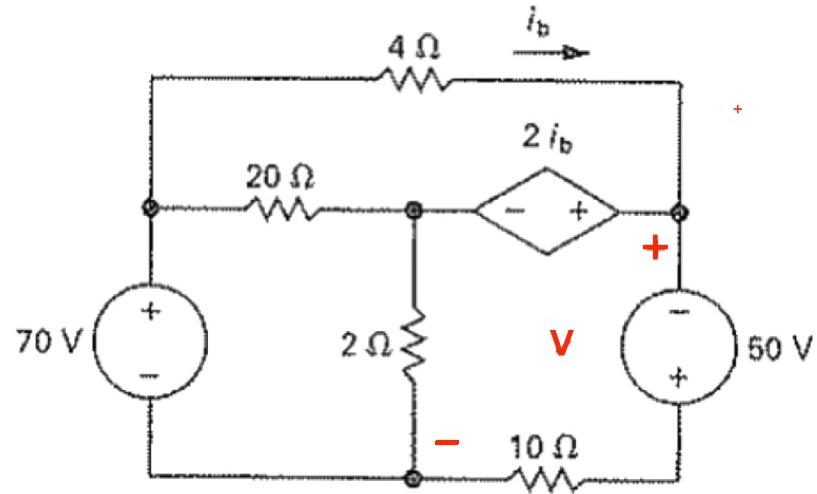


Node – 1

basic concepts

General Methods to Analyze Circuits

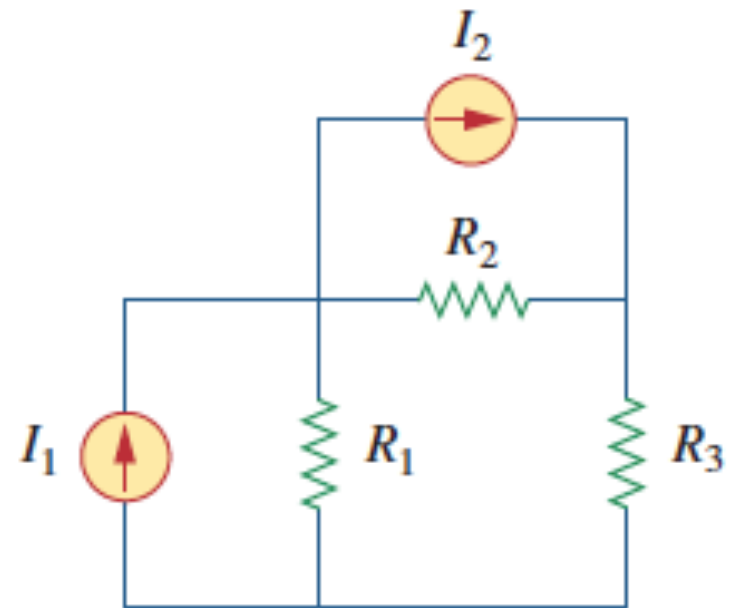
- What to do first?
 - KVL?
 - KCL?
 - Ohm's Law?



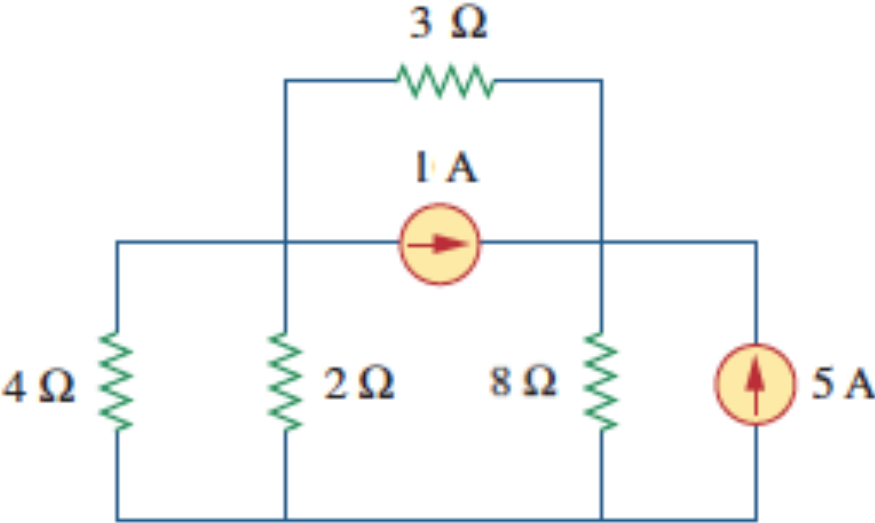
- We need a more direct approach:
 - Nodal analysis (KCL based)
 - Mesh analysis (KVL based, **end of semester**)
- Review appendix A (also online)

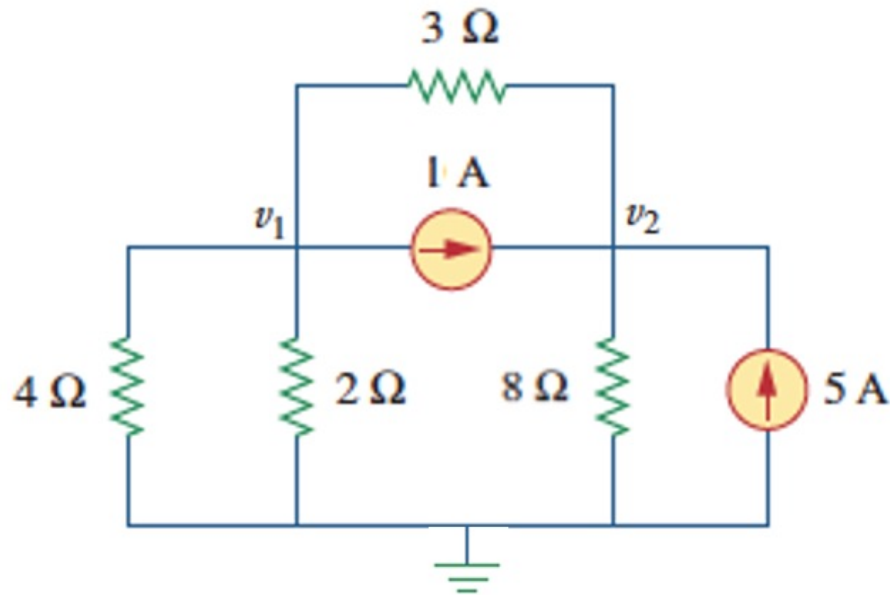
Node Analysis

- Consider a circuit with current sources and resistors only
- Identify nodes
 - Select one as “ground”
 - Label others
 - Write KCL on these other nodes
 - Use Ohm’s Law for current in the resistive branches
 - Solve resulting equations



Example (details repeated on next slide)





$$\frac{v_1}{2} + \frac{v_1}{4} + \frac{v_1 - v_2}{3} + 1 = 0$$

$$\frac{v_2}{8} + \frac{v_2 - v_1}{3} = 1 + 5$$

$$6v_1 + 3v_1 + 4v_1 - 4v_2 = -12$$

$$3v_2 + 8v_2 - 8v_1 = 144$$

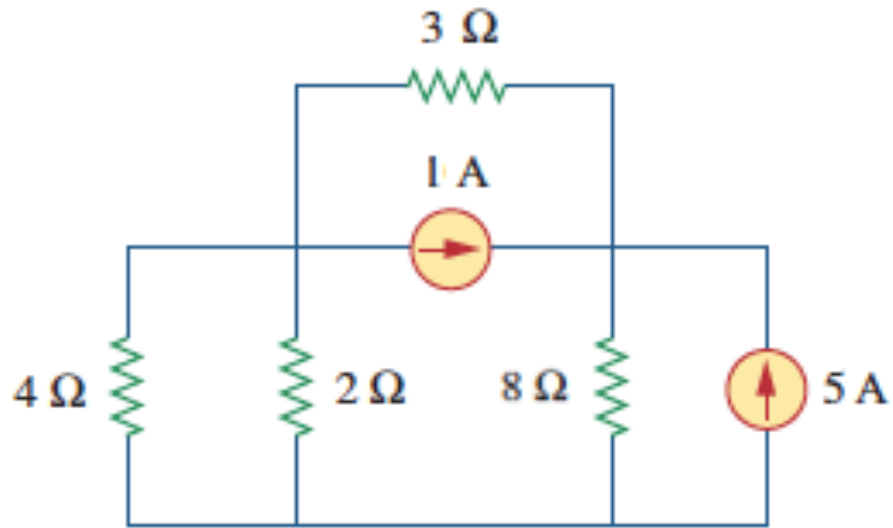
$$13v_1 - 4v_2 = -12$$

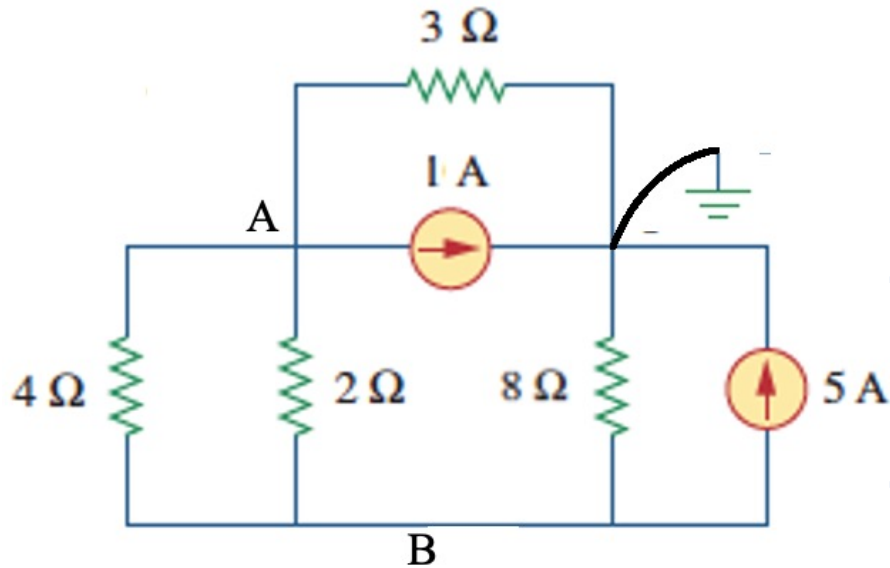
$$-8v_1 + 11v_2 = 144$$

$$v_1 = \frac{\begin{vmatrix} -12 & -4 \\ 144 & 11 \end{vmatrix}}{\begin{vmatrix} 13 & -4 \\ -8 & 11 \end{vmatrix}} = \frac{-132 + 576}{143 - 32} = \frac{444}{111} = 4 \text{ volts}$$

$$v_2 = \frac{\begin{vmatrix} 13 & -12 \\ -8 & 144 \end{vmatrix}}{\begin{vmatrix} 13 & -4 \\ -8 & 11 \end{vmatrix}} = \frac{1872 - 96}{111} = \frac{1776}{111} = 16 \text{ volts}$$

Example (same circuit, change ground to top right, details on next slide)





$$\frac{A - B}{2} + \frac{A - B}{4} + \frac{A}{3} + 1 = 0$$

$$\frac{B - A}{4} + \frac{B - A}{2} + \frac{B}{8} + 5 = 0$$

$$6A - 6B + 3A - 3B + 4A = -12$$

$$2B - 2A + 4B - 4A + B = -40$$

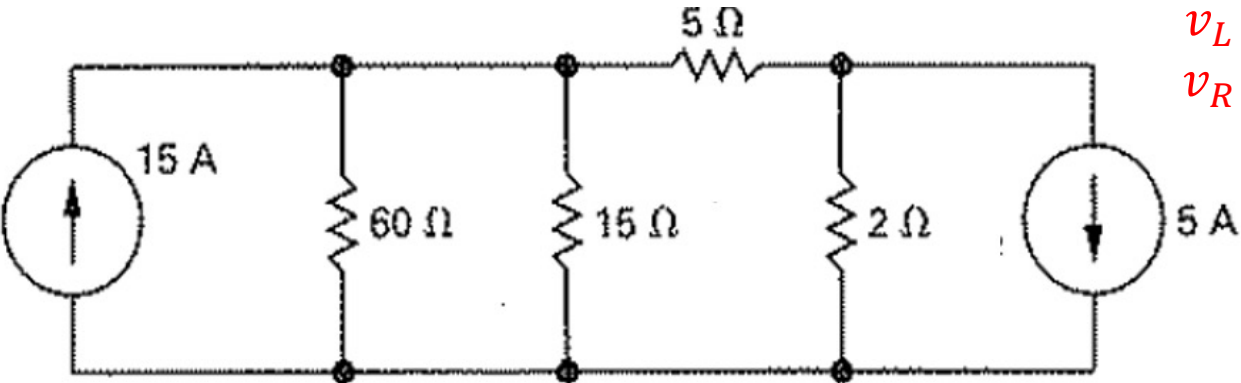
$$13A - 9B = -12$$

$$-6A + 7B = -40$$

$$A = \frac{\begin{vmatrix} -12 & -9 \\ -40 & 7 \end{vmatrix}}{\begin{vmatrix} 13 & -9 \\ -6 & 7 \end{vmatrix}} = \frac{-84 - 360}{91 - 54} = \frac{-444}{37} = -12 \text{ volts}$$

$$B = \frac{\begin{vmatrix} 13 & -12 \\ -6 & -40 \end{vmatrix}}{\begin{vmatrix} 13 & -9 \\ -6 & 7 \end{vmatrix}} = \frac{-520 - 72}{35} = \frac{-592}{37} = -16 \text{ volts}$$

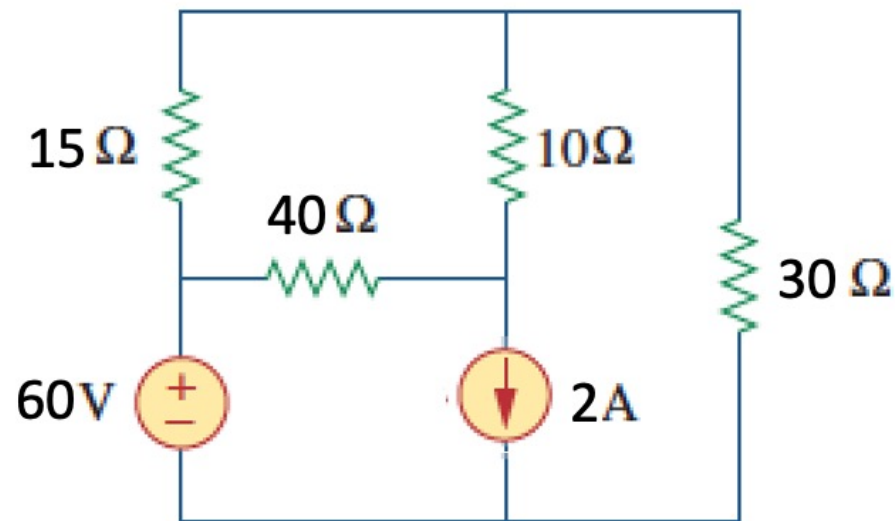
Example:



$v_L = 60 V$
 $v_R = 10 V$

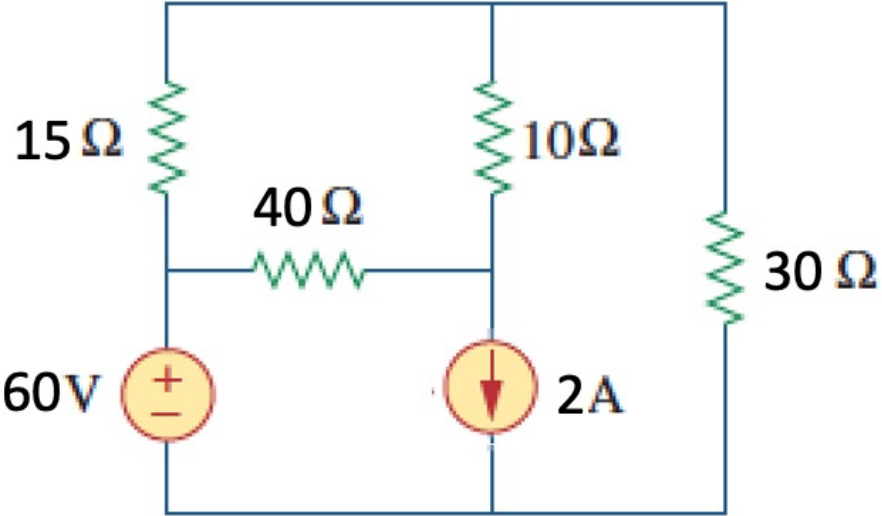
Extension #1 – a V-only branch

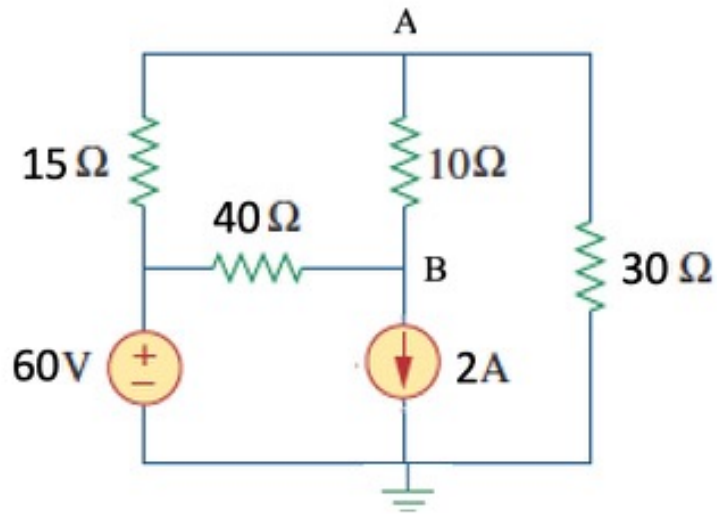
- Consider:



- **IF** connected to ground, it's just one less node voltage to worry about

Example (details on next slide)





$$\frac{A - 60}{15} + \frac{A - B}{10} + \frac{A}{30} = 0$$

$$\frac{B - 60}{40} + \frac{B - A}{10} + 2 = 0$$

$$6A - 3B = 120$$

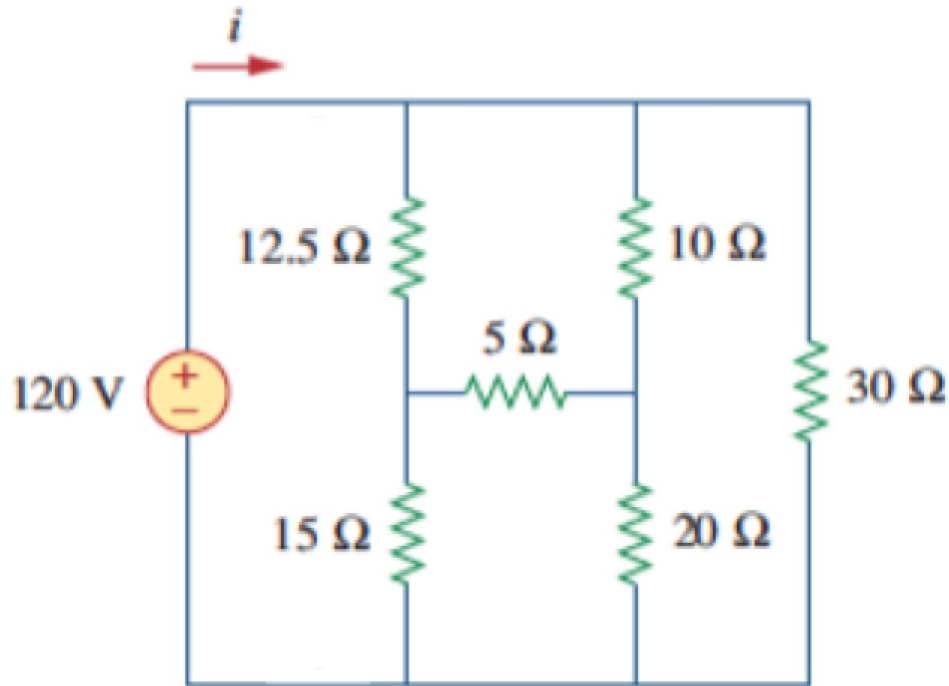
$$-4A + 5B = -20$$

$$A = 30 \text{ volts}$$

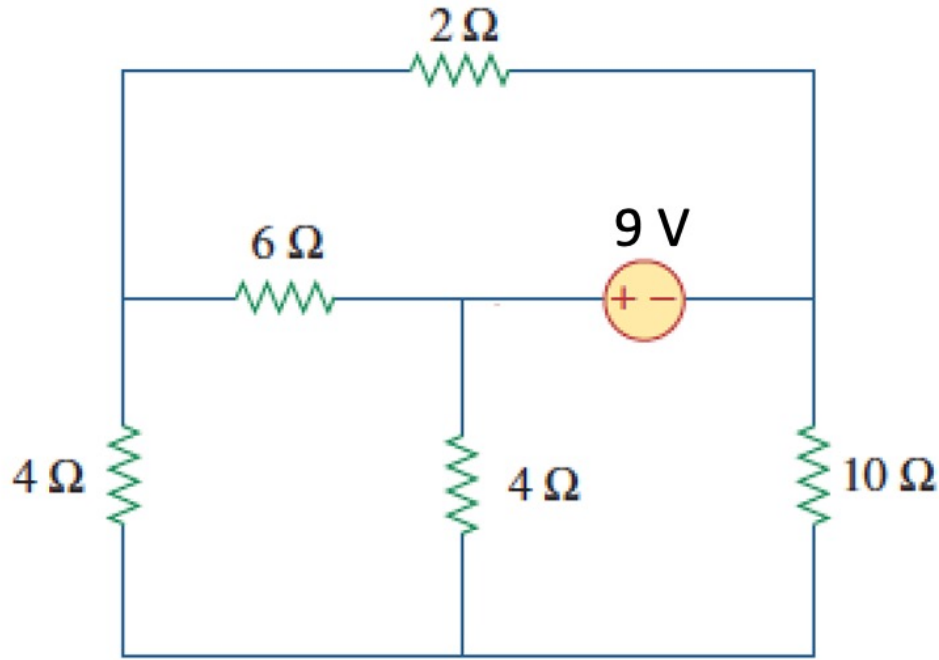
$$B = 20 \text{ volts}$$

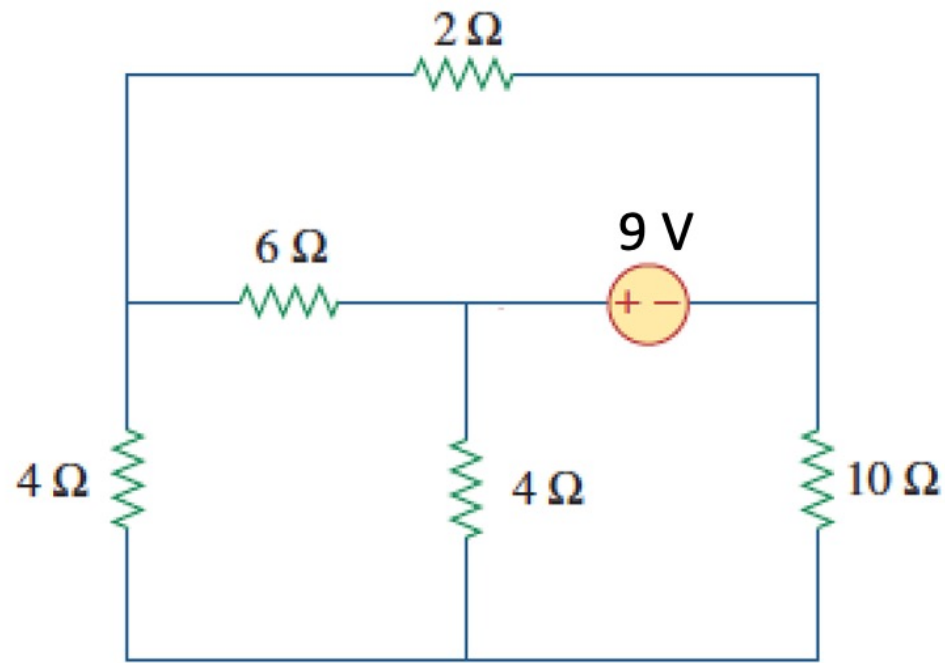
Example from Delta-Wye transformations

$$\begin{aligned}v_L &= 70.8 \text{ V} \\v_R &= 74.8 \text{ V} \\i &= 12.5 \text{ A}\end{aligned}$$



Example: recall that we can place ground as needed; put it on the right and solve for left and bottom

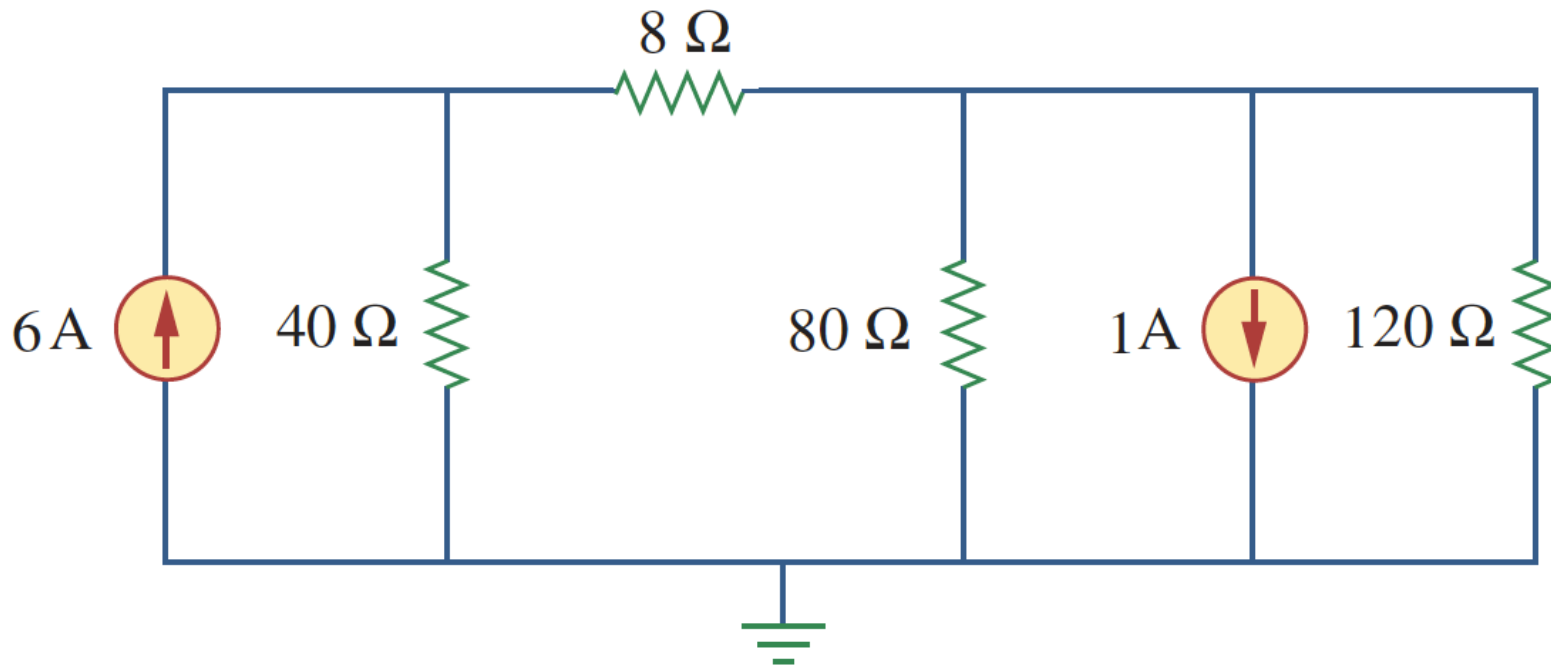




$$v_L = 3\text{ V}$$
$$v_B = 5\text{ V}$$

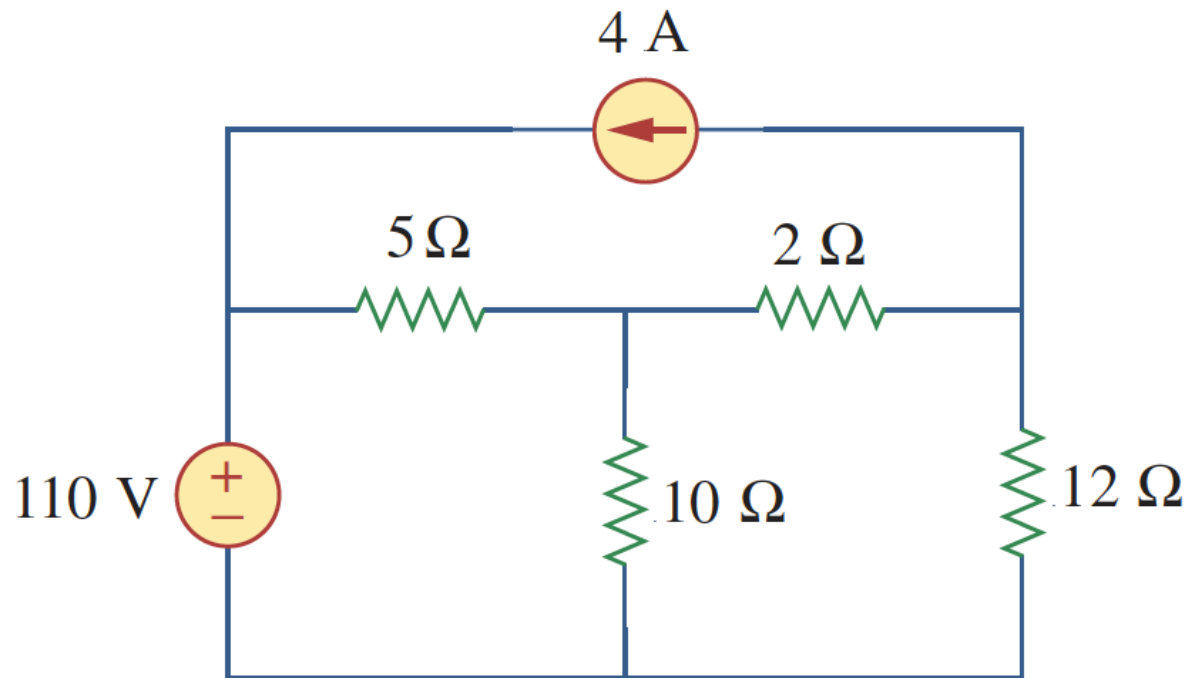
120 V, 96 V

Practice problem: find the nodes voltages to the left and right of the 8 Ω resistor



50 V, 36 V

Practice problem: assuming ground on the bottom, find the nodes voltages to the left and right of the 2 Ω resistor



70 V, 60 V

Practice problem: find the nodes voltages to the left and right of the $10\text{ k}\Omega$ resistor, ground at the bottom

